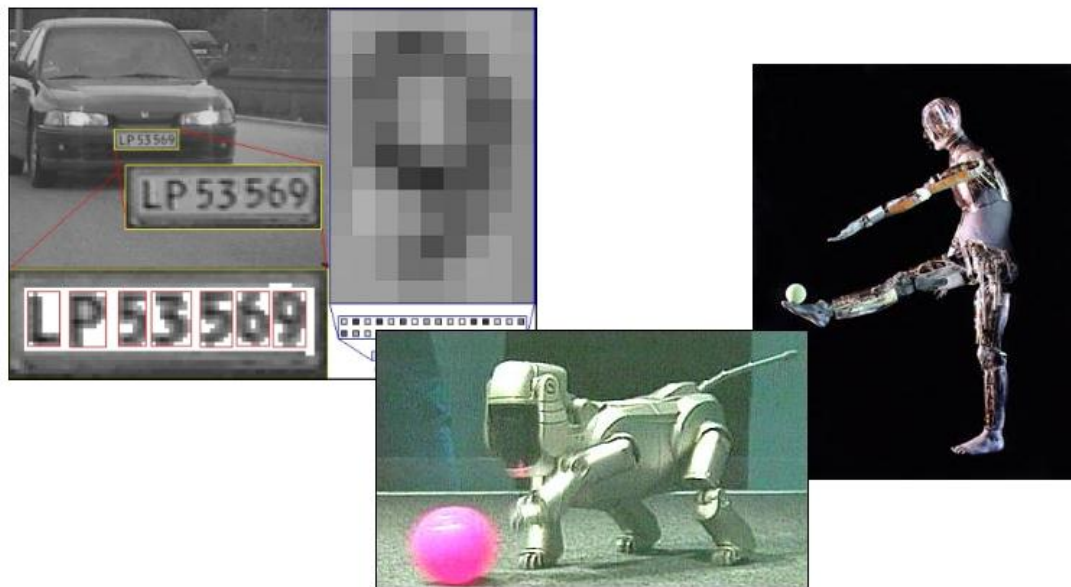




Распознавание образов

Константин Третьяков

<http://kt.era.ee>

DevClub
27.04.2011

STACC
Software Technology and
Applications Competence Center



Data mining,

Data analysis, Statistical analysis,

Pattern discovery, Statistical learning,

Machine learning, Predictive analytics,

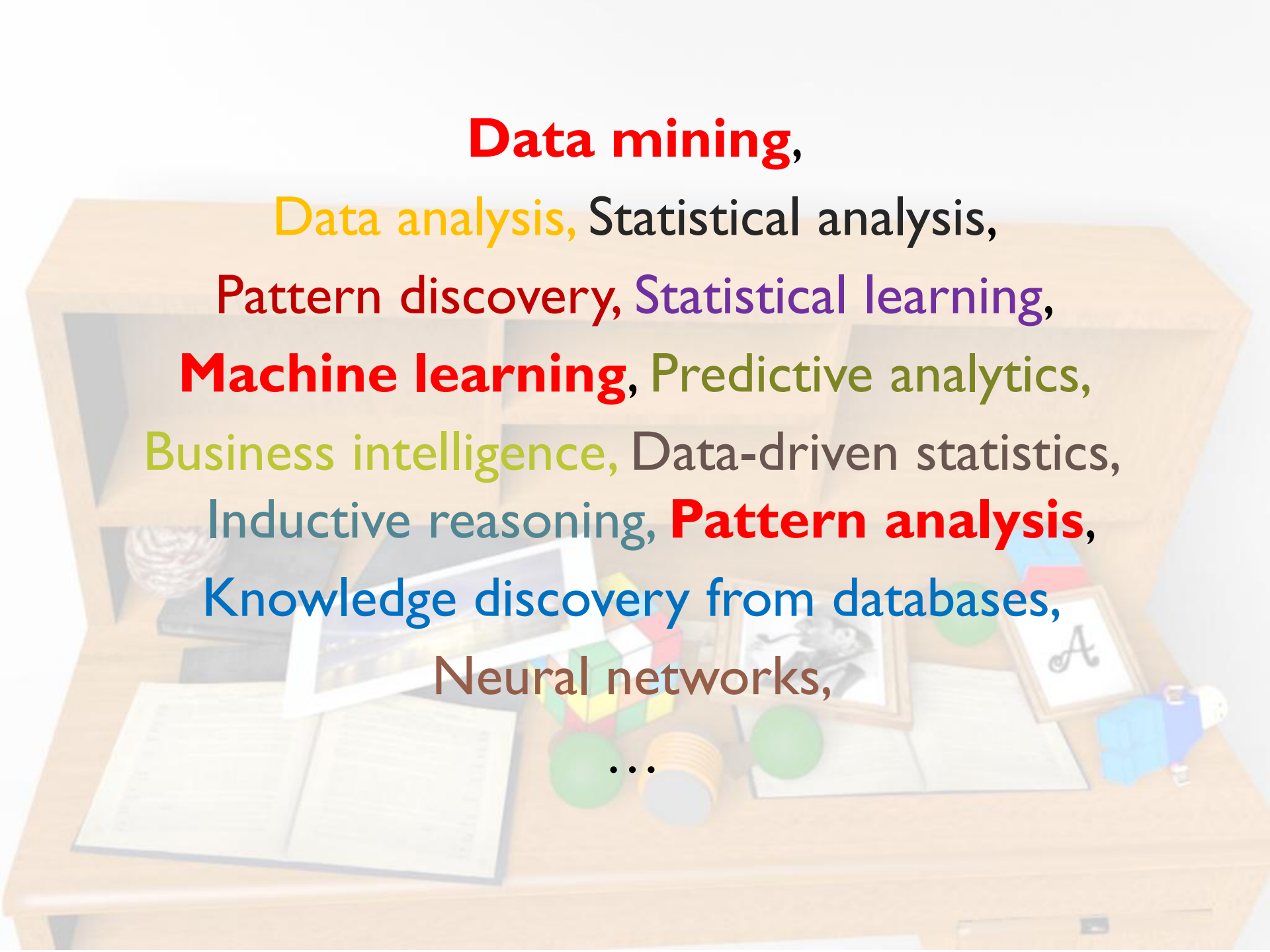
Business intelligence, Data-driven statistics,

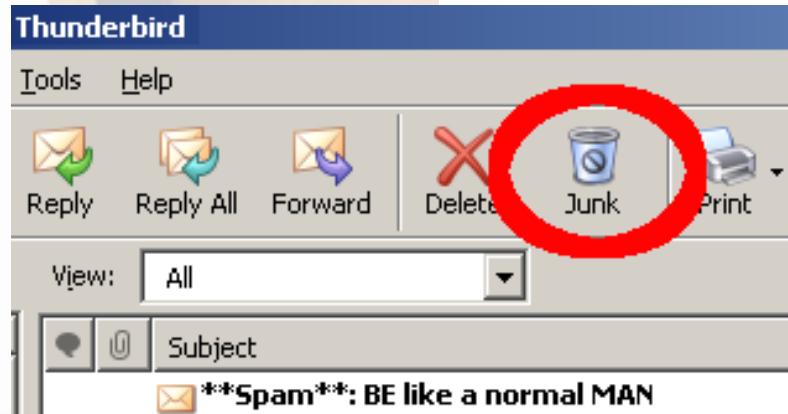
Inductive reasoning, **Pattern analysis,**

Knowledge discovery from databases,

Neural networks,

...



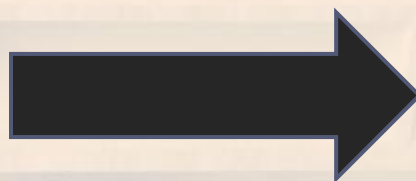
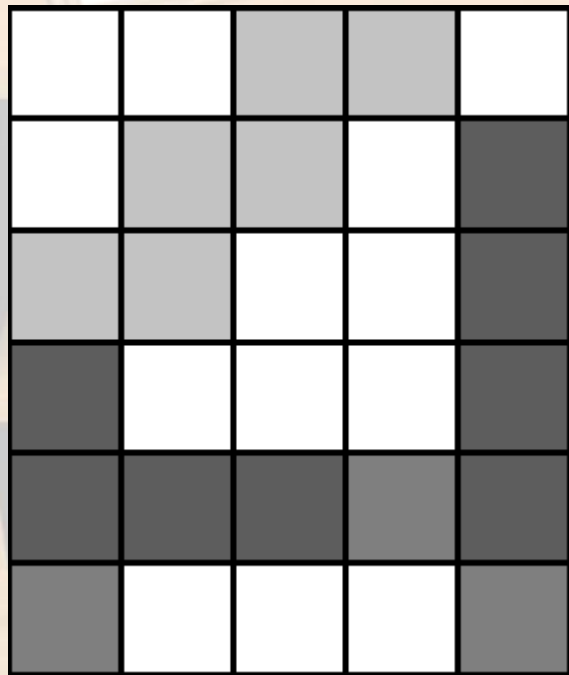


Google translate

NETFLIX

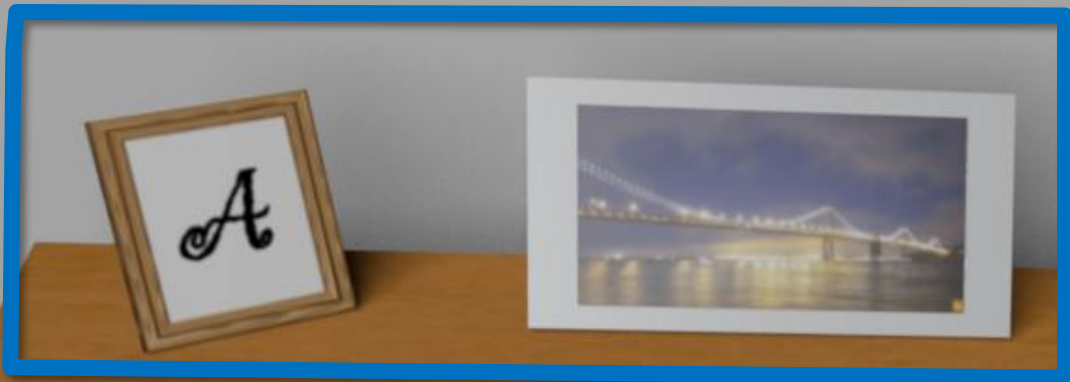






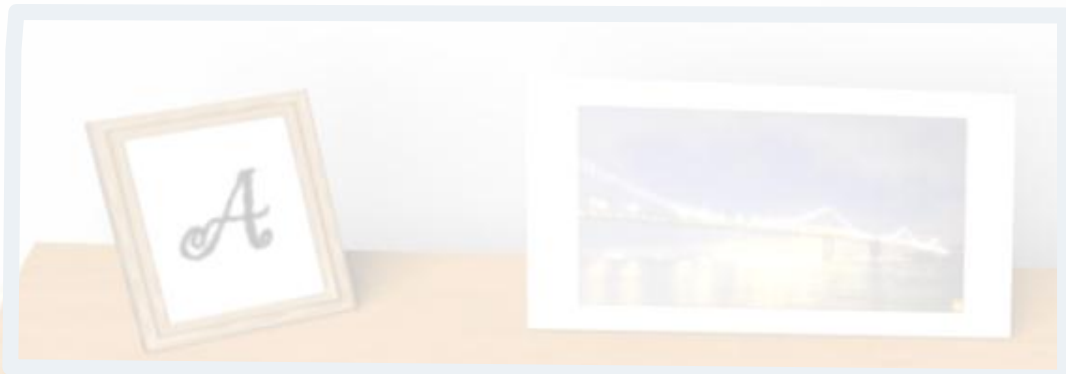
A



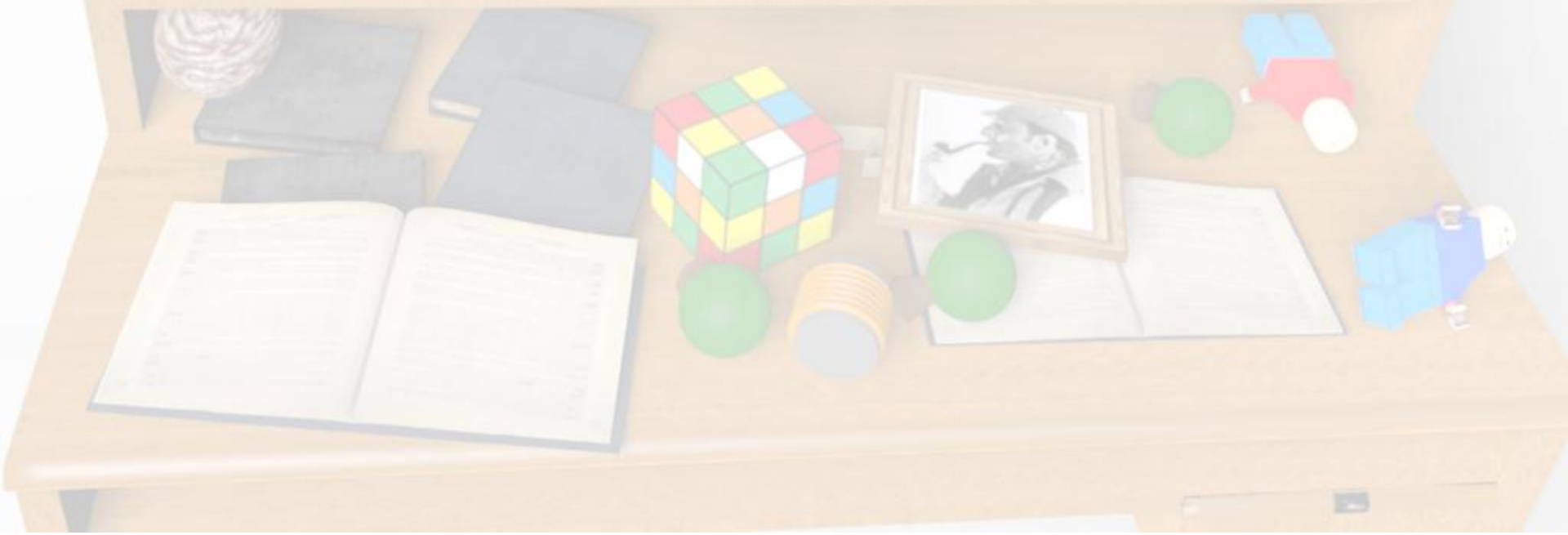


Плохо формализуемые задачи





Плохо формализуемые задачи



A

A

B

Плохо формализуемые задачи

A

B

B

A

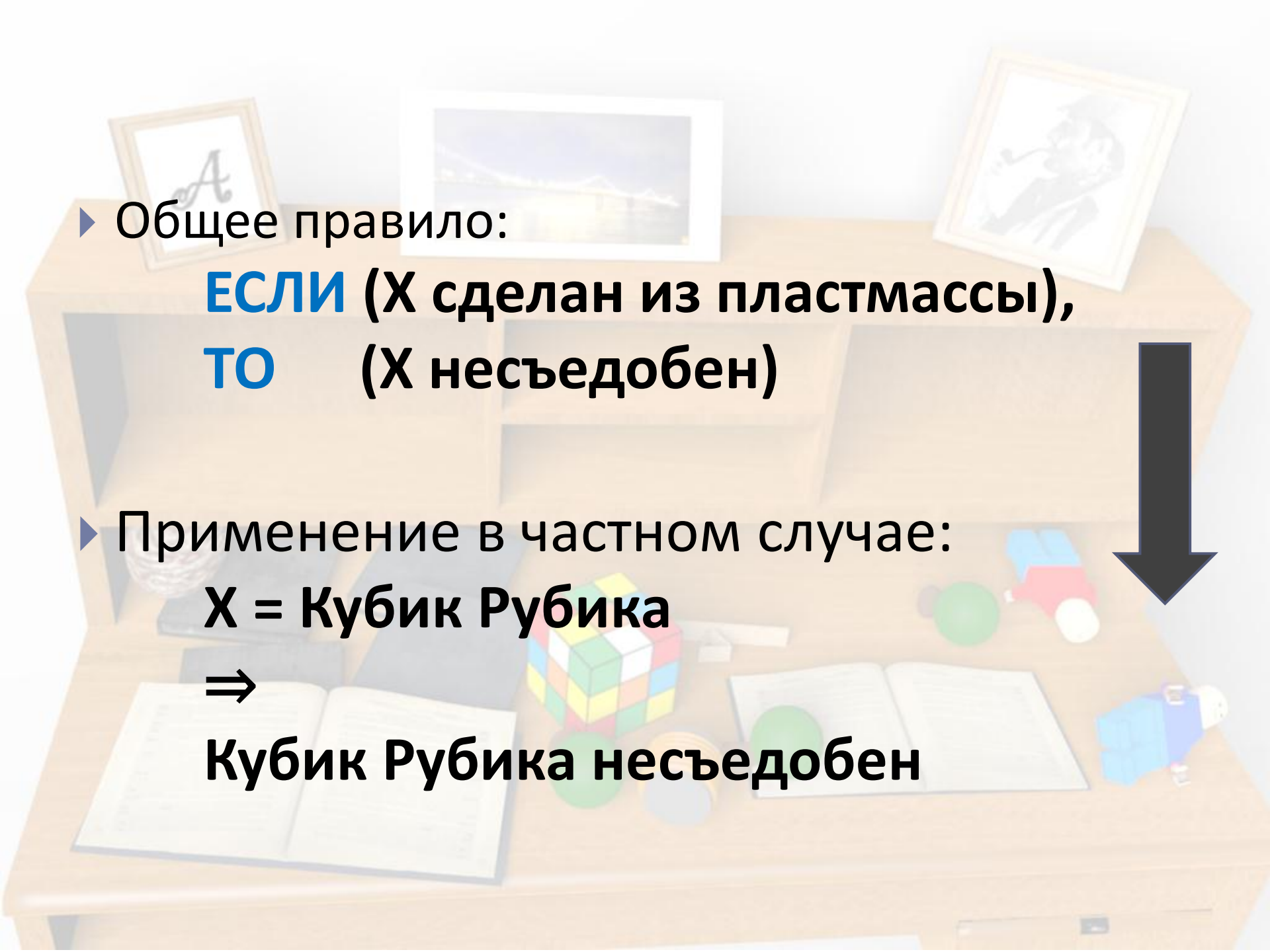
A

A

B





- 
- Общее правило:

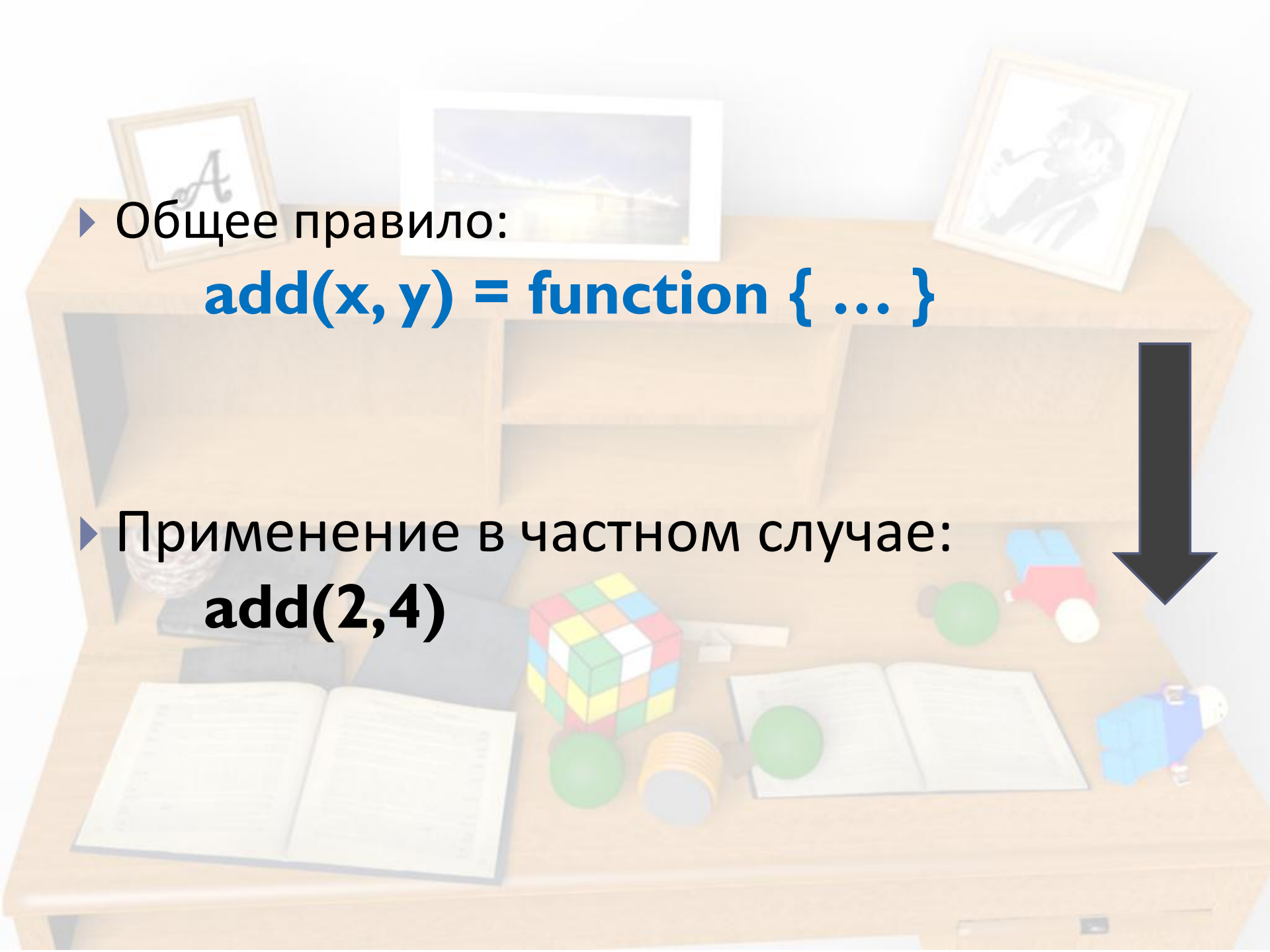
ЕСЛИ (X сделан из пластмассы),
ТО (X несъедобен)

- Применение в частном случае:

X = Кубик Рубика

⇒

Кубик Рубика несъедобен

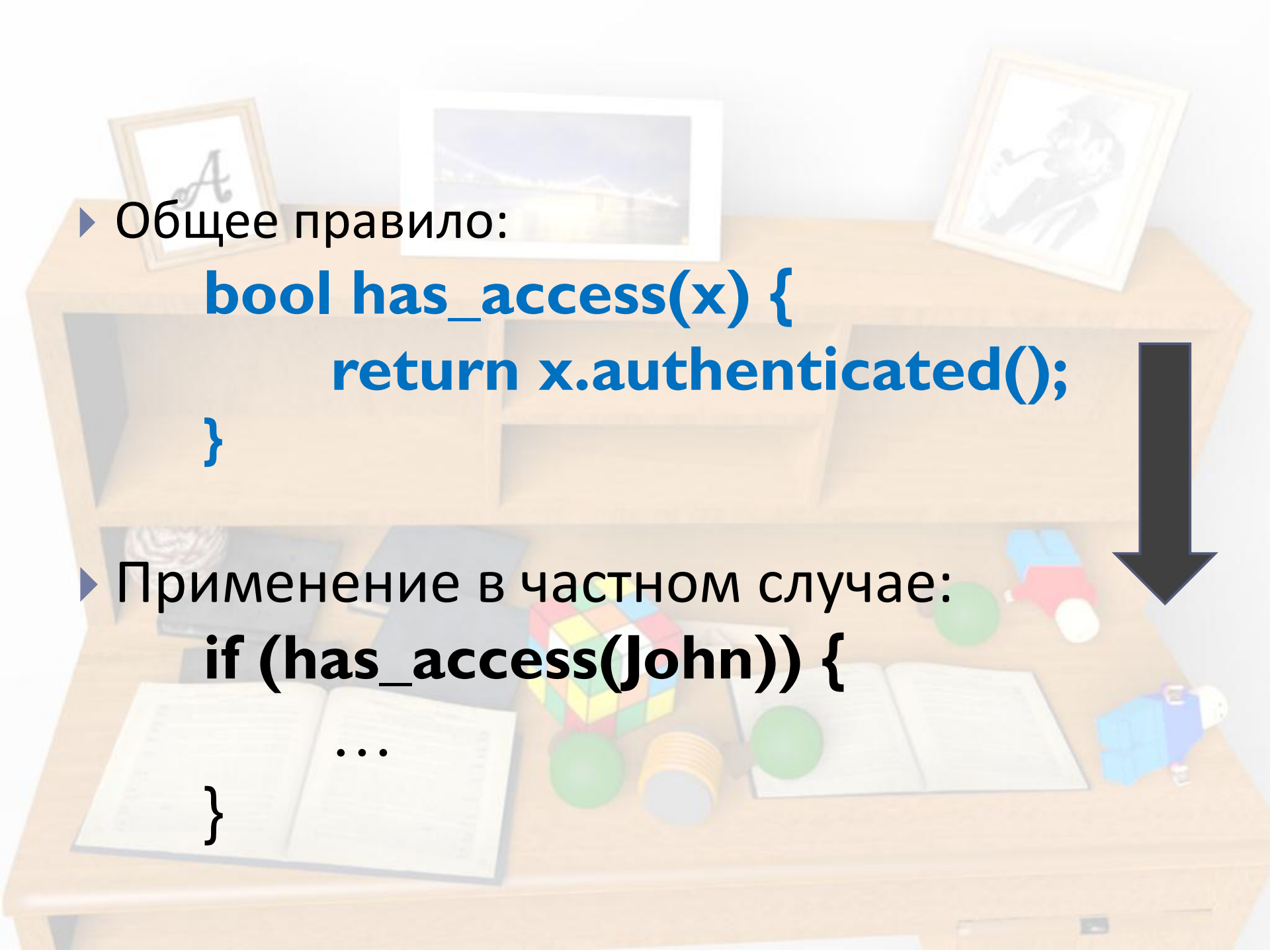
- 
- Общее правило:

add(x, y) = function { ... }

- Применение в частном случае:

add(2,4)



- 
- Общее правило:

```
bool has_access(x) {  
    return x.authenticated();  
}
```

- Применение в частном случае:

```
if (has_access(John)) {  
    ...  
}
```



- Общее правило:

```
bool has_access(x) {  
    ?  
}
```

- Частные случаи:

```
has_access(John) = True  
has_access(Jane) = True  
has_access(Mike) = False
```

...



- Общее правило:

```
bool has_access(x) {  
    ?  
}
```

- Частные случаи:

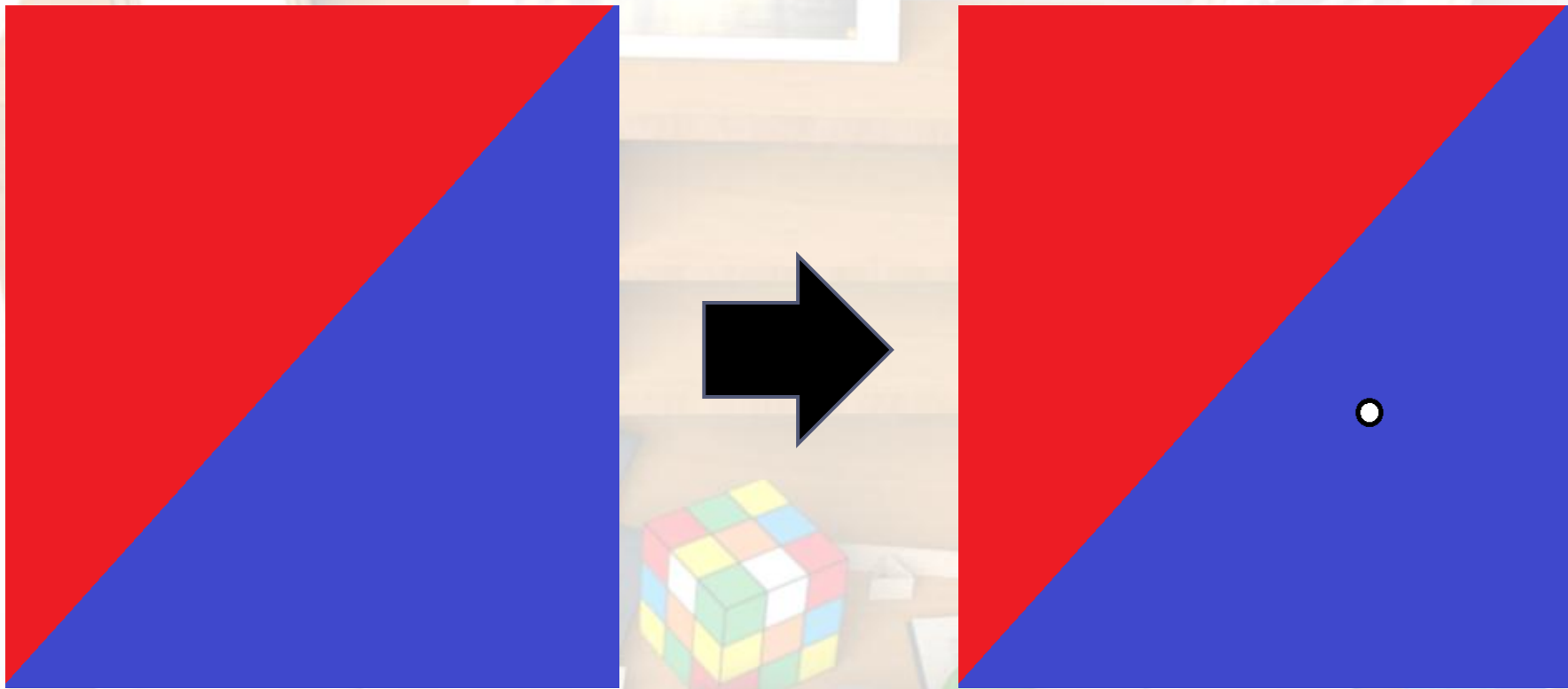
```
has_access(John) = True  
has_access(Jane) = True  
has_access(Mike) = False
```

...

Индукция

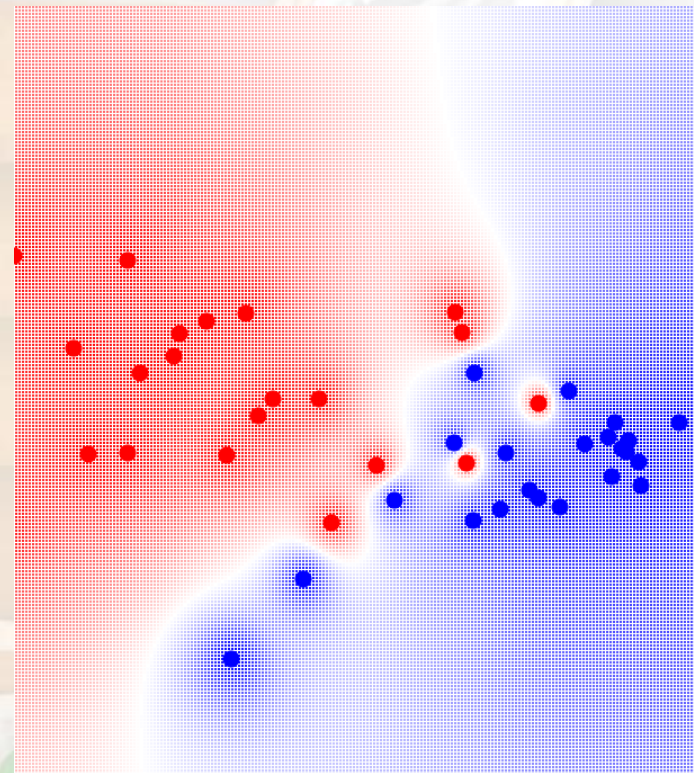
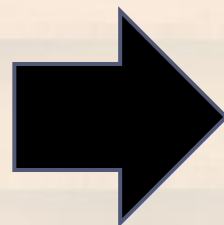
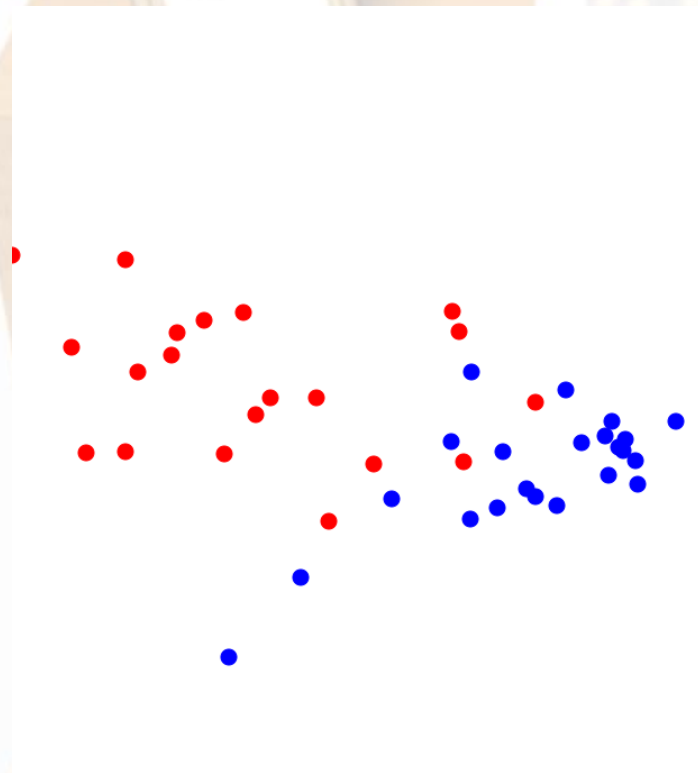


Дедукция



Известно общее правило, нужно принять решение в частном случае

Индукция

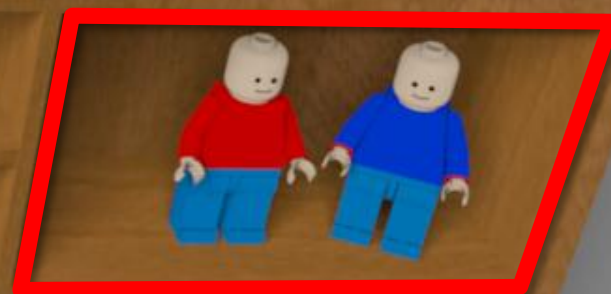
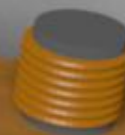


Известны частные случаи, нужно найти общее правило



Дедукция и индукция





**Классификация
по аналогии**



MNIST dataset

- ▶ <http://yann.lecun.com/exdb/mnist/>
- ▶ Картинки рукописных цифр, 28 x 28



MNIST dataset

```
from PIL import Image
from glob import glob
from numpy import array

def load_image(filename):
    img = Image.open(filename)
    return array(
        [ord(char) for char in img.tostring()]
    )
```

MNIST dataset

10 000 файлов *.png

```
files = glob("*.png")
```

Загружаем данные

```
images = [load_image(file) for file in files]
```

102.1.png -> "1" (класс)

```
labels = [file.split(".")[1] for file in files]
```

Возьмем 1000 картинок

```
training_set = images[0:1000]
```

```
training_labels = labels[0:1000]
```

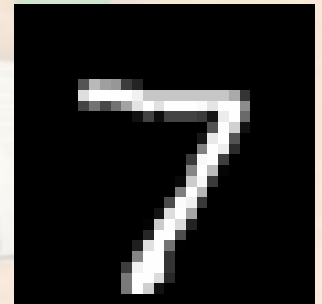

MNIST dataset

```
> training_set[0]
```

```
array([ 0,  0,  0, ...,  
       254, 241, 198, ...])
```

```
> training_labels[0]
```

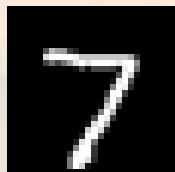
'7'



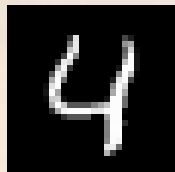
Метод ближайшего соседа

Training set

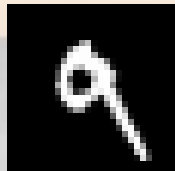
7



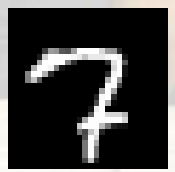
4



9



7



4



4

Метод ближайшего соседа

```
def classify(img):  
    similarities =  
        [similarity(img, p) for p in training_set]  
    i = similarities.index(max(similarities))  
    return training_labels[i]
```

Метод ближайшего соседа

```
def classify(img):  
    similarities =  
        [similarity(img, p) for p in training_set]  
    i = similarities.index(max(similarities))  
    return training_labels[i]
```

```
def similarity(img1, img2):  
    return -sum(abs(img1 - img2))
```


Проверим

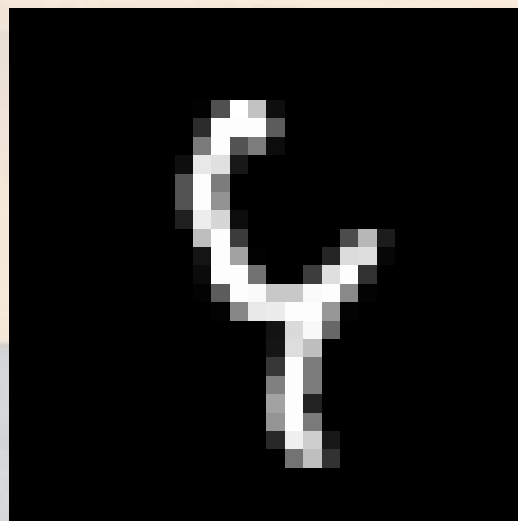
```
test_set      = images[1000:2000]  
test_labels = labels[1000:2000]
```

```
predicted_class = map(classify, test_set)
```

```
n_successes =  
    sum(array(predicted_class) ==  
        array(test_labels))
```

=> 860/1000

9 или 4?



Scikit-learn

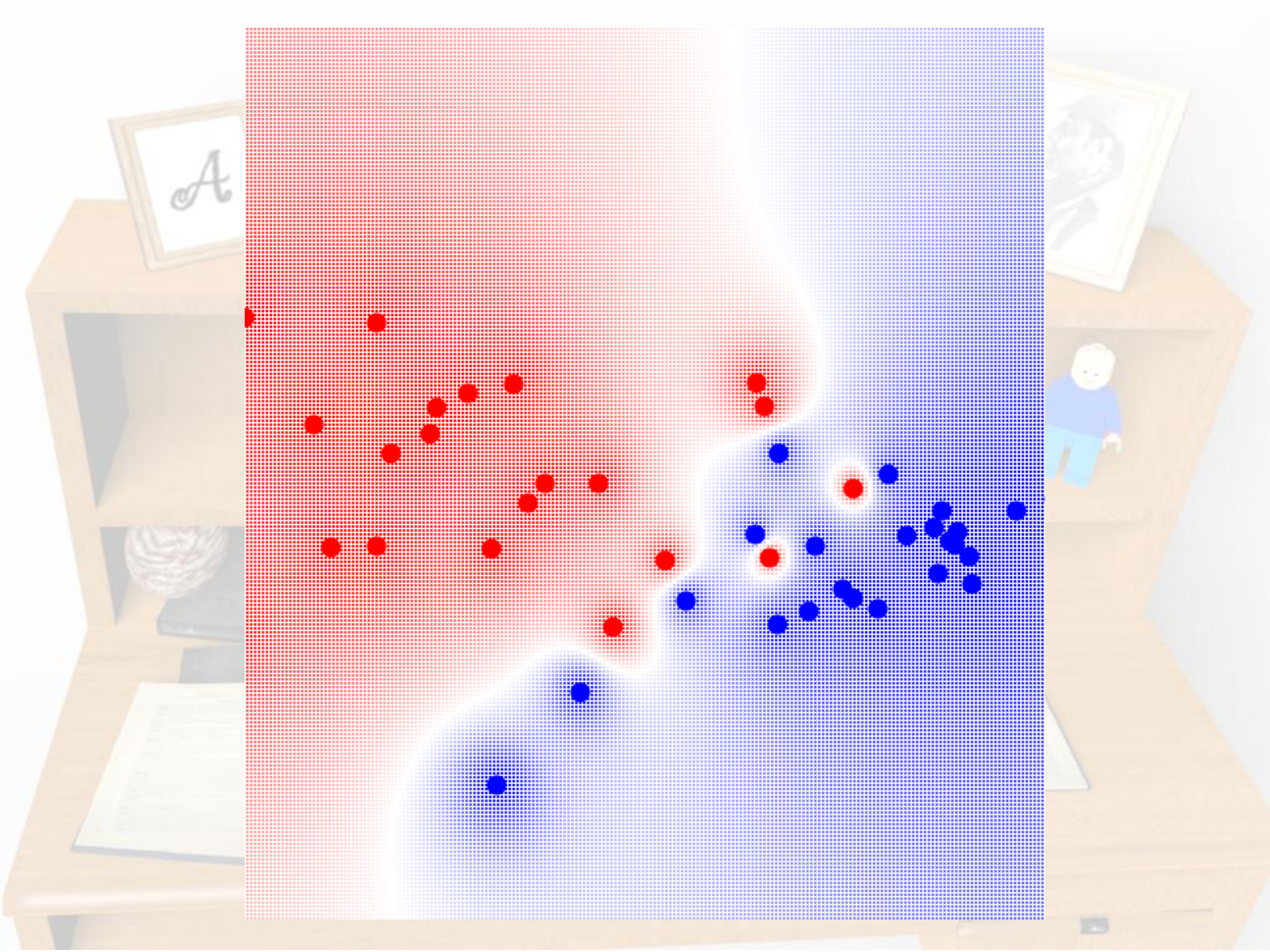
<http://scikit-learn.sourceforge.net/>

```
from scikits.learn.neighbors import  
NeighborsClassifier
```

```
clf = NeighborsClassifier(n_neighbors=1)  
clf.fit(training_set, training_labels)
```

```
predicted_class = clf.predict(test_set)
```

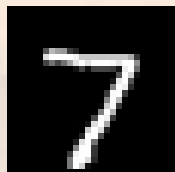
=> 869/1000



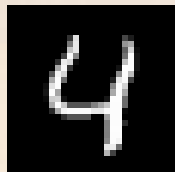
Метод ближайшего соседа

Training set

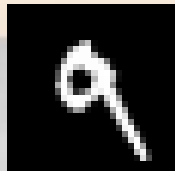
7



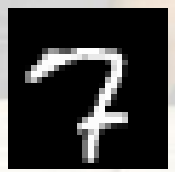
4



9



7



4

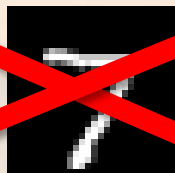


4

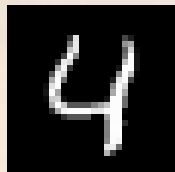
Некоторые примеры можно выкинуть

Training set

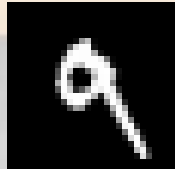
7



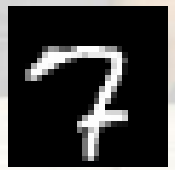
4



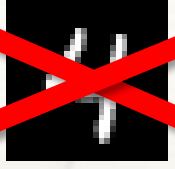
9



7



4

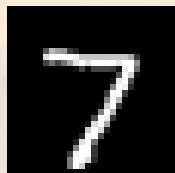


4

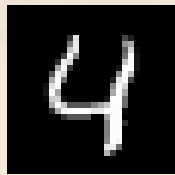
Еще хитрее – добавить «веса»

Training set

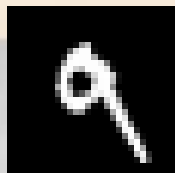
7



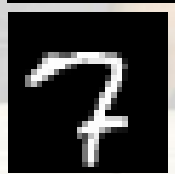
4



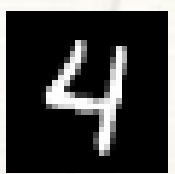
9



7



4



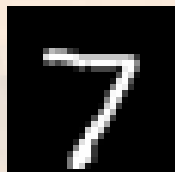
4

Еще хитрее – добавить «веса»

Training set

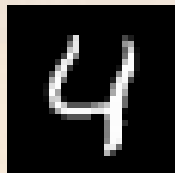
0.0

7



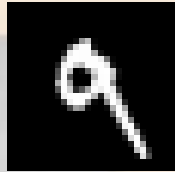
0.9

4



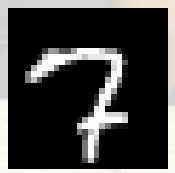
1.1

9



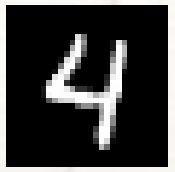
2.0

7



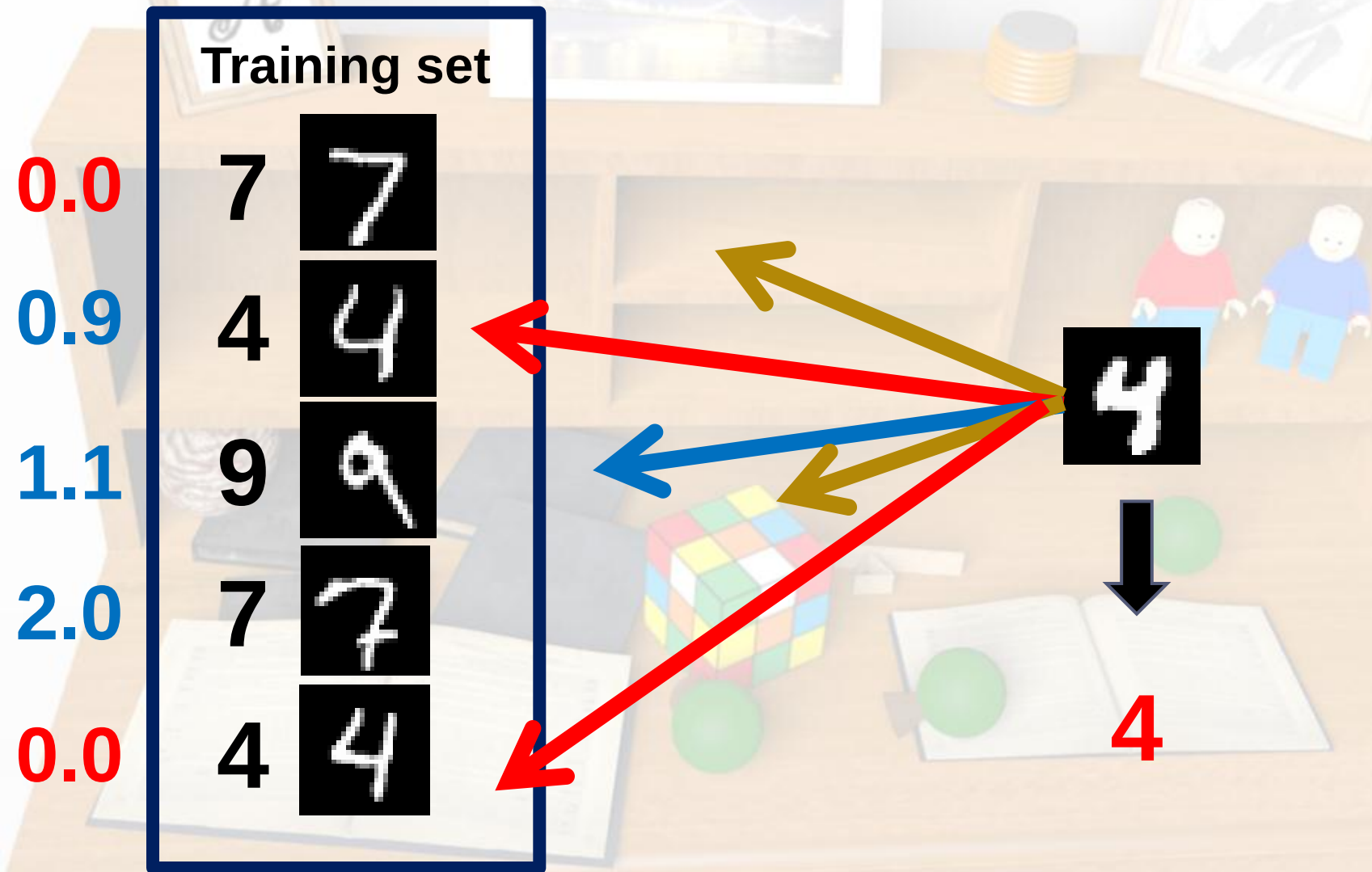
0.0

4



4

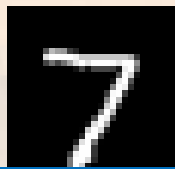
Вместо максимума, можно суммировать



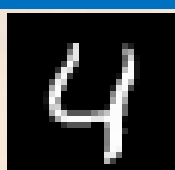
Вместо максимума, можно суммировать

Training set

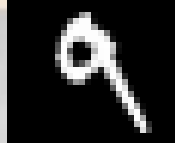
7



4



9



7



4



evidence(img, 4) =

0.9 * similarity(img, tr[1])

+

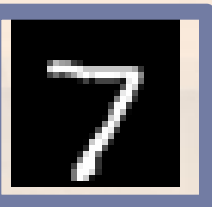
0.0 * similarity(img, tr[4])

= 34.0

Вместо максимума, можно суммировать

Training set

7



4



9



7



4



`evidence(img, 7) =`

`0.0 * similarity(img, tr[0])`

`+`

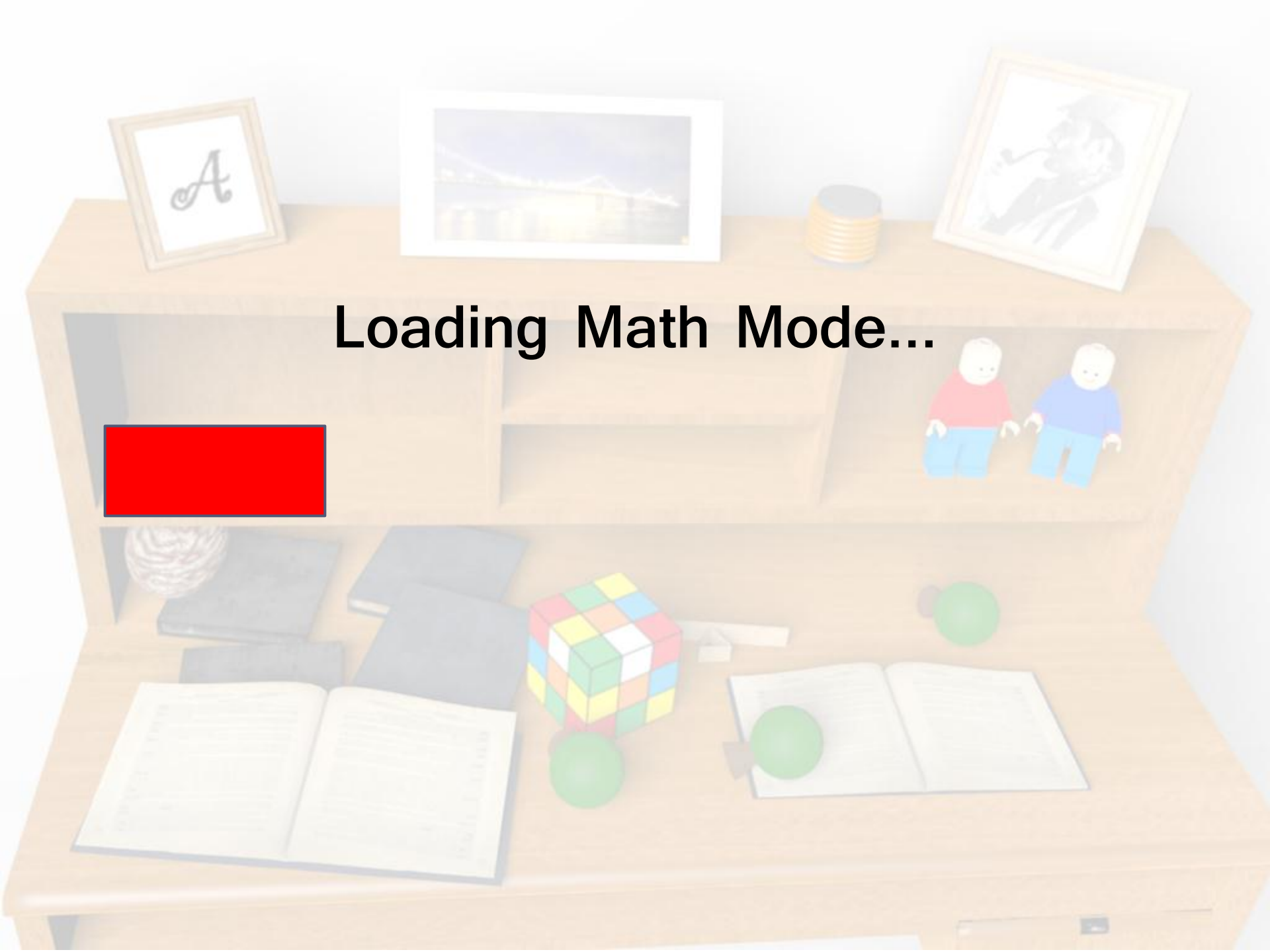
`2.0 * similarity(img, tr[3])`

`= 20.0`

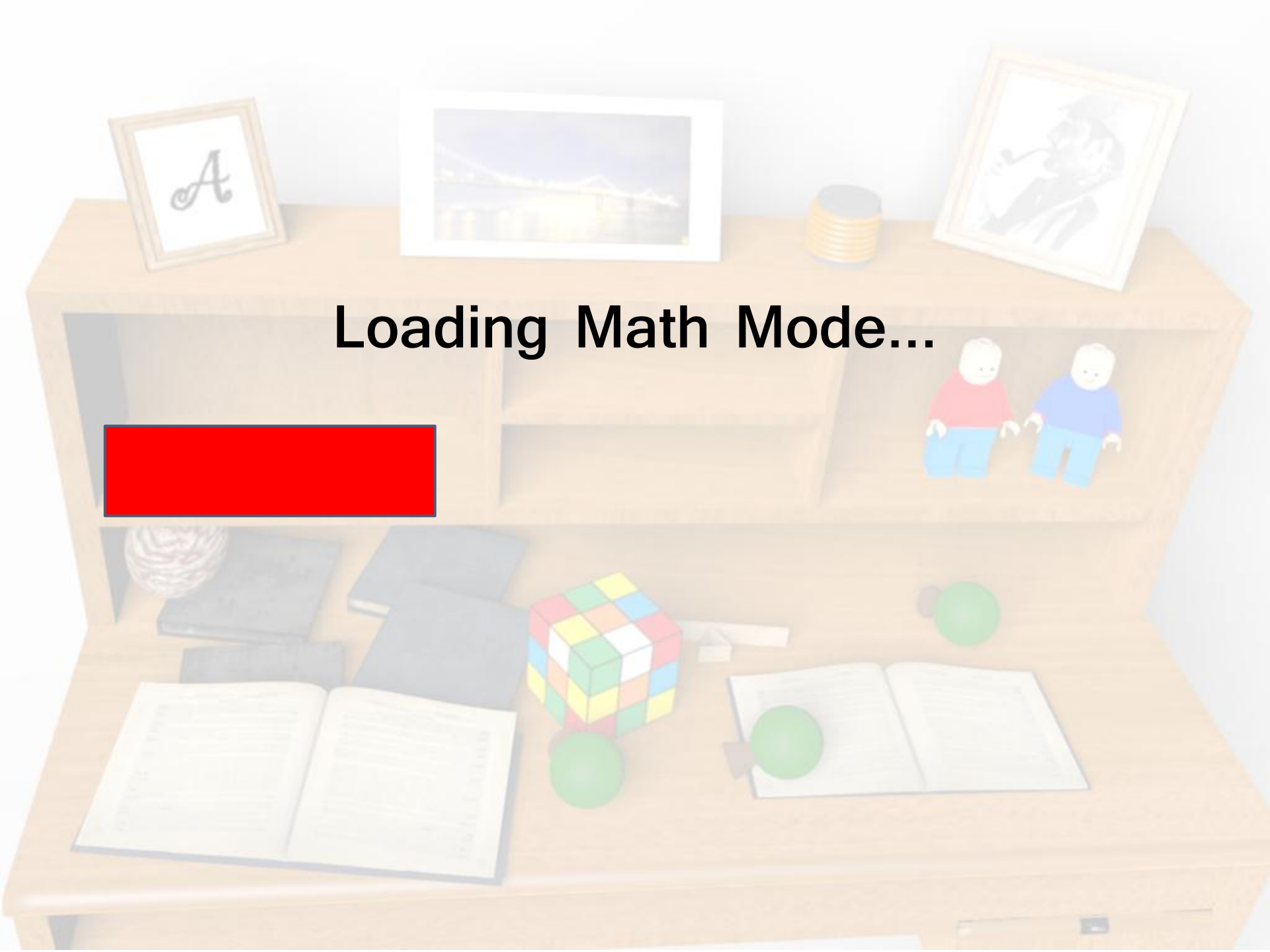
Loading Math Mode...



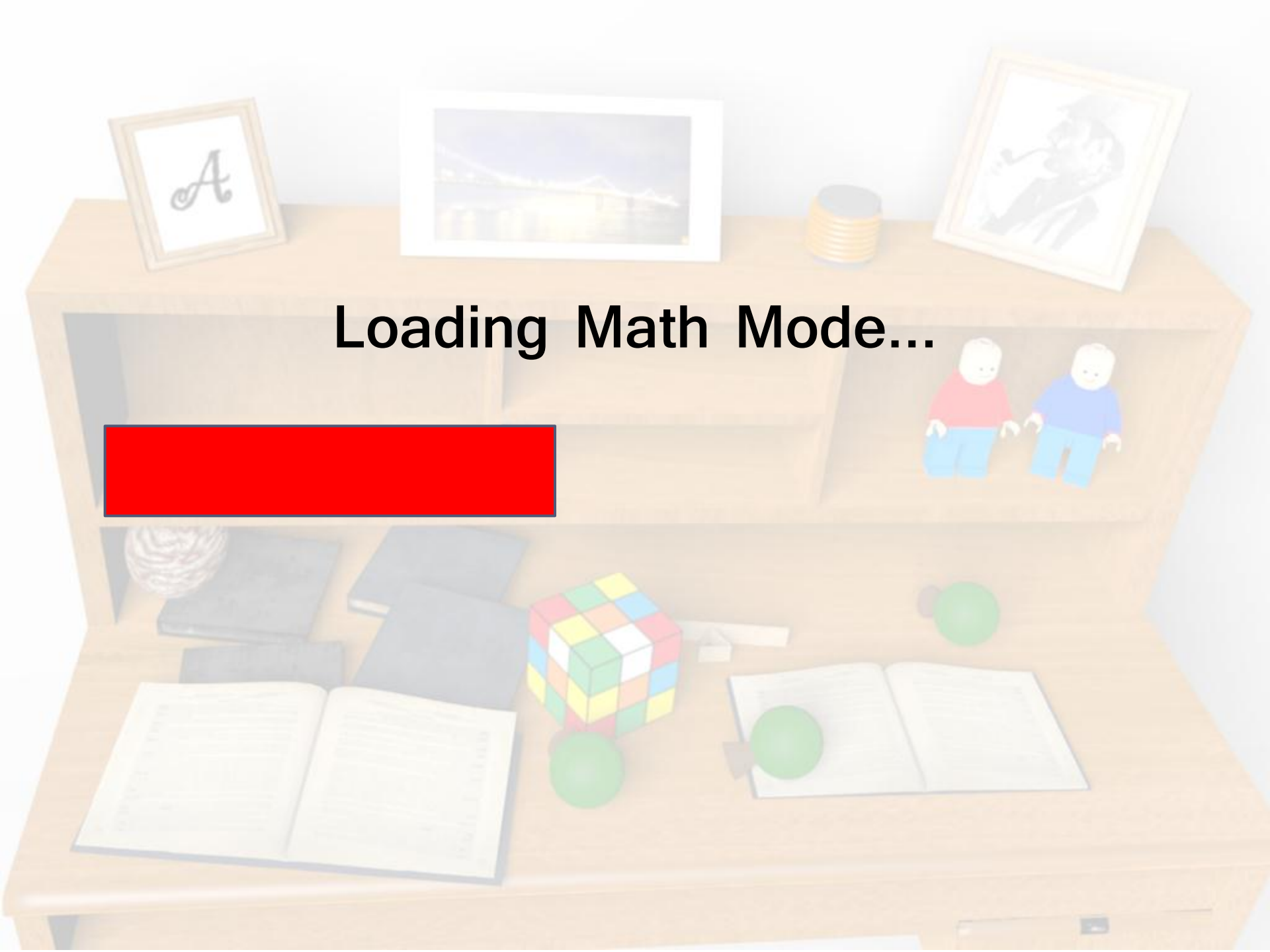
Loading Math Mode...



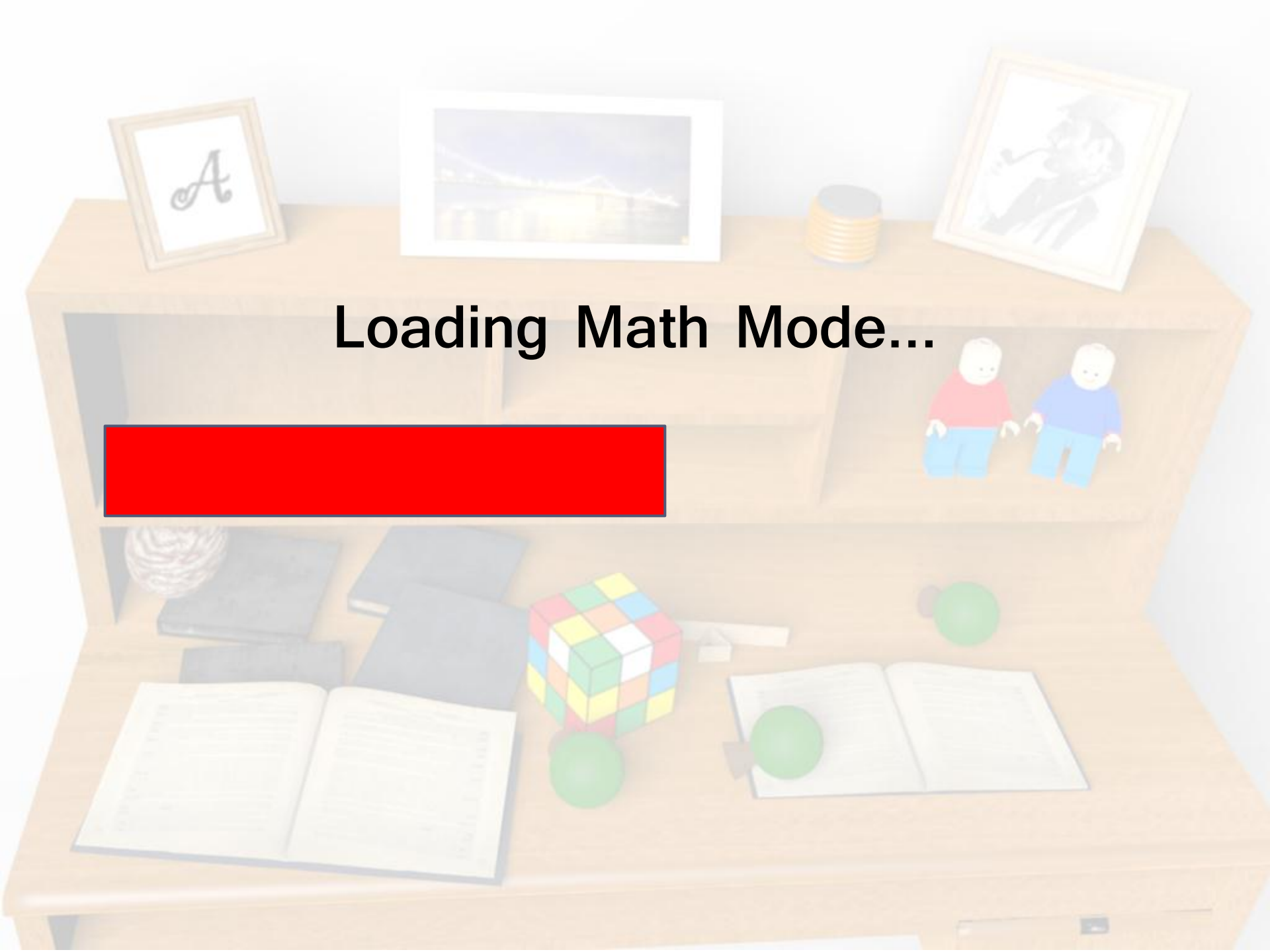
Loading Math Mode...



Loading Math Mode...



Loading Math Mode...



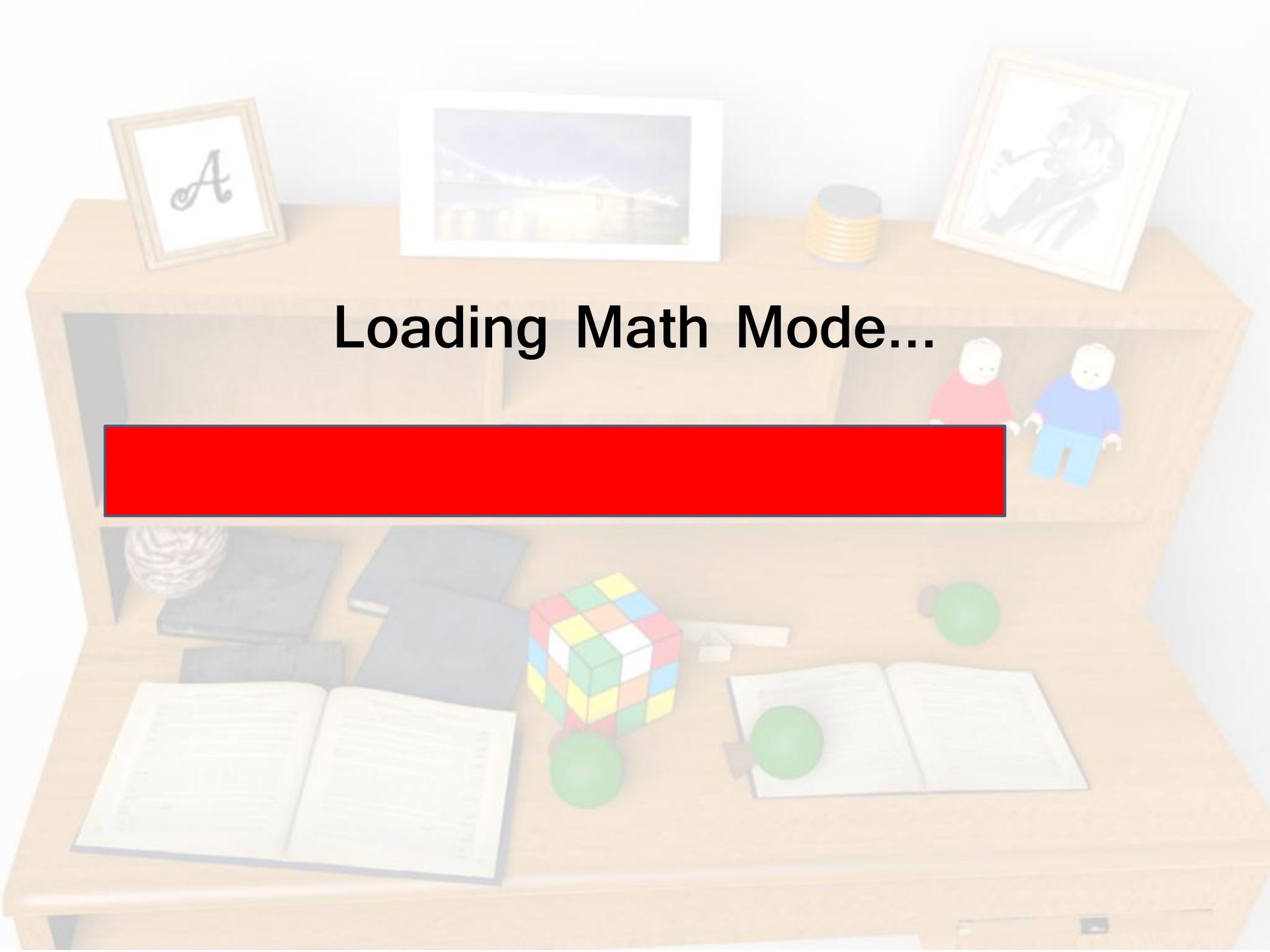
Loading Math Mode...

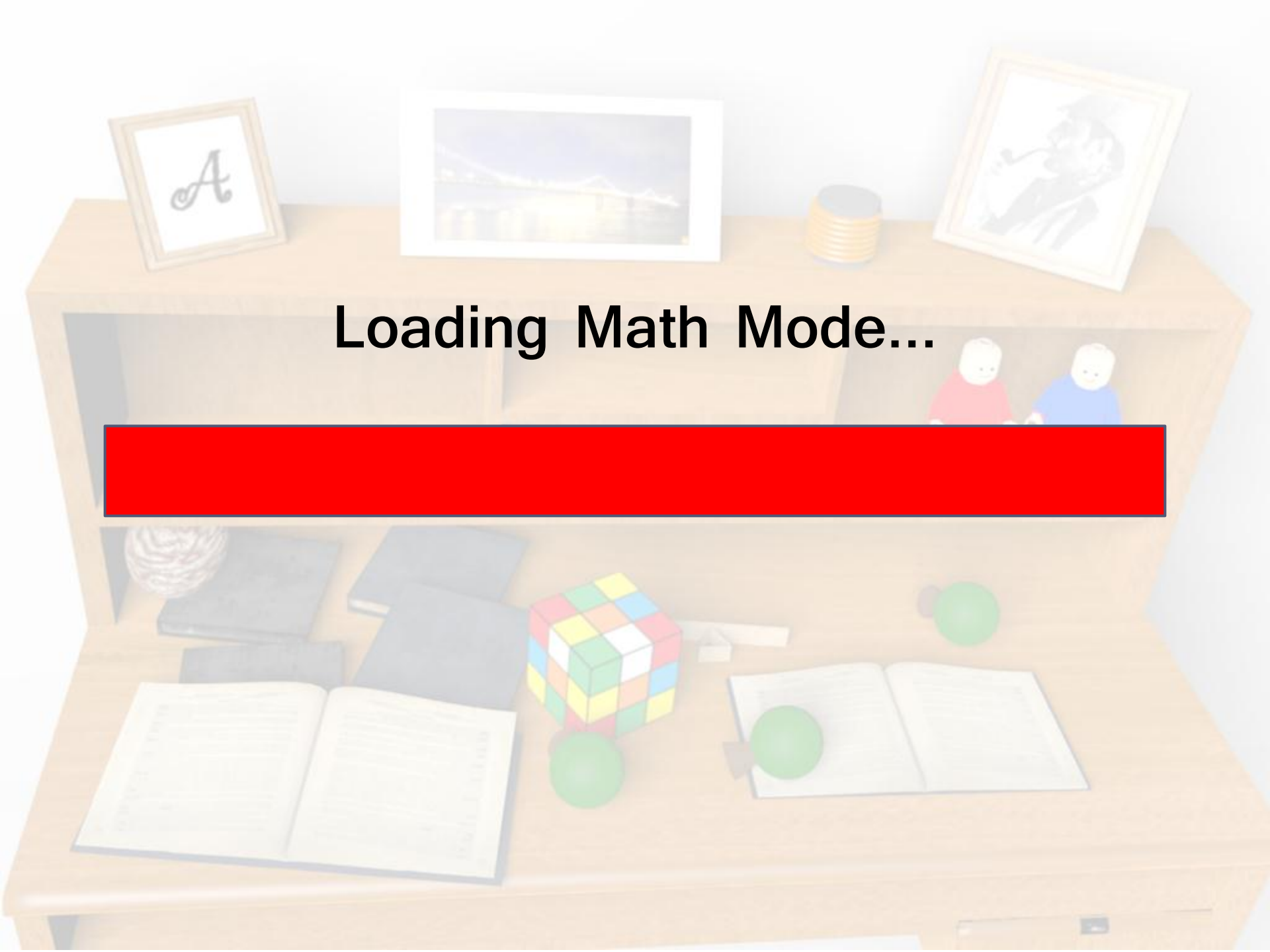


Loading Math Mode...

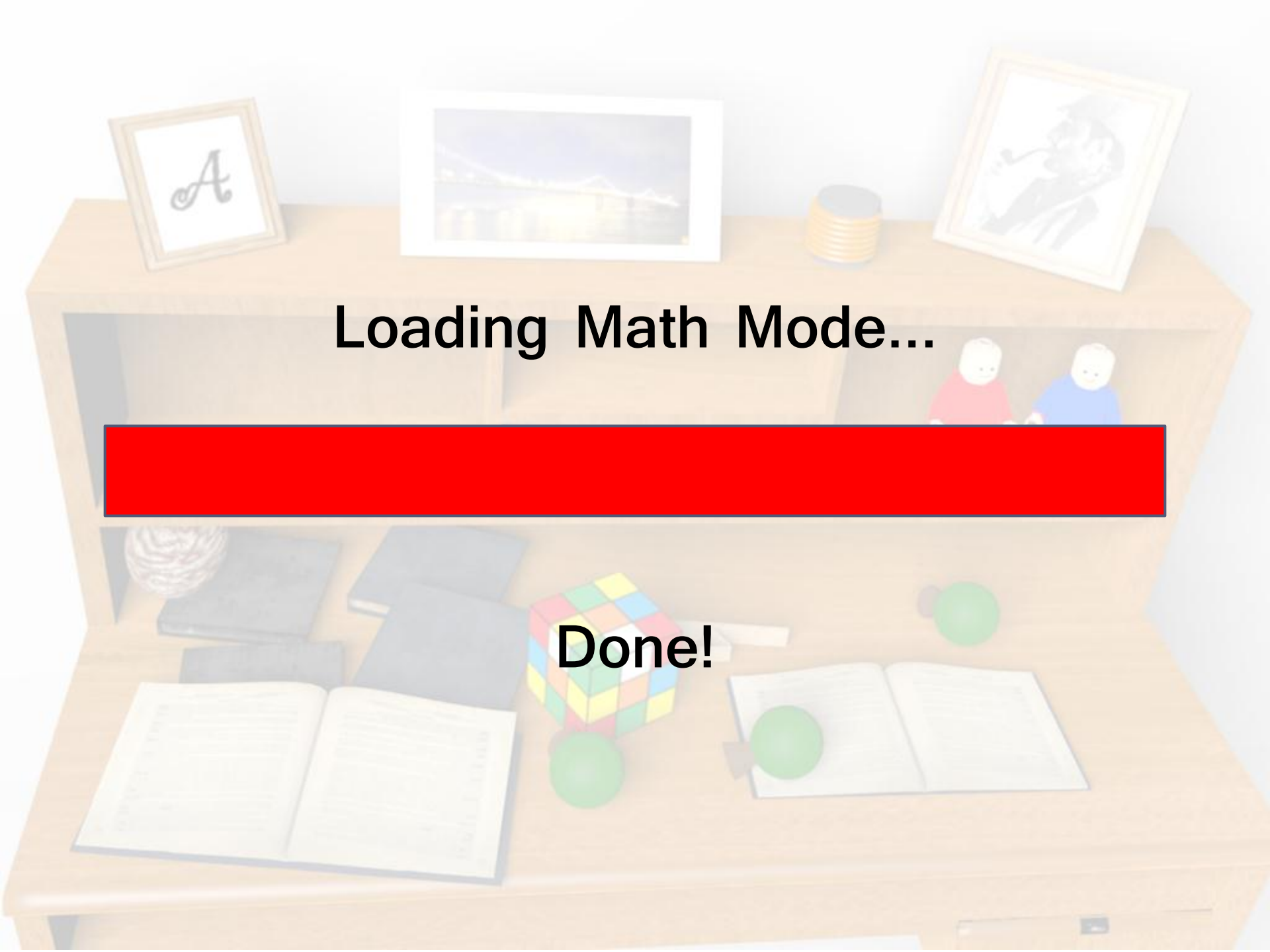


Loading Math Mode...



A wooden desk with various items. On the top shelf, there are three framed pictures: a letter 'A', a bridge at night, and a portrait of a man. Next to the portrait is a stack of yellow and grey discs. In the middle shelf, there are two small white figures, one in a red shirt and one in a blue shirt. A large red rectangular box with a black border is placed in front of the middle shelf. On the bottom shelf, there are several books, a Rubik's cube, a small white pyramid, and two green spheres. One book is open on the left, and another is open on the right.

Loading Math Mode...

A wooden desk with various items on it. On the top shelf, there are three framed pictures: a letter 'A', a landscape with a bridge, and a portrait of a man. A stack of yellow and grey discs is also on the shelf. Two small white figures are on the right. A large red bar is in the center. On the bottom shelf, there are several books, a Rubik's cube, and two green spheres. The text 'Loading Math Mode...' is overlaid on the red bar.

Loading Math Mode...

Done!

Общий вид

$$f(x) = \sum_i y_i w_i K(x_i, x)$$

Но как найти веса?

$$f(x) = \sum_i y_i w_i K(x_i, x)$$

- ▶ Найдем те, при которых **частота ошибок предсказания** на независимом множестве **минимальна**.

$$\mathbf{w} = \operatorname{argmin}_{\mathbf{w}} \operatorname{Error}(\mathbf{f}, \mathbf{w}, \text{Data})$$

Но как найти веса?

$$f(x) = \sum_i y_i w_i K(x_i, x)$$

- ▶ Найдем те, при которых **мера ошибки предсказания** на независимом множестве **минимальна**.

$$\mathbf{w} = \operatorname{argmin}_{\mathbf{w}} \operatorname{Error}^*(f, \mathbf{w}, \text{Data})$$

Но как найти веса?

$$f(x) = \sum_i y_i w_i K(x_i, x)$$

- ▶ Найдем те, при которых **мера ошибки предсказания** на независимом множестве **минимальна + много нулевых весов**

$$w = \operatorname{argmin}_w \operatorname{Error}^*(f, w, \text{Data}) + \operatorname{Complexity}(w)$$

Support Vector Machine

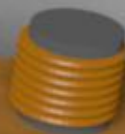
```
from sklearn.learn.svm import SVC
```

```
clf = SVC(kernel='linear')
```

```
clf.fit(training_set, training_labels)
```

```
predicted_class = clf.predict(test_set)
```

=> 877/1000





Классификация
по аналогии:
k-NN
SVM
RBF

Поиск ближайшего соседа

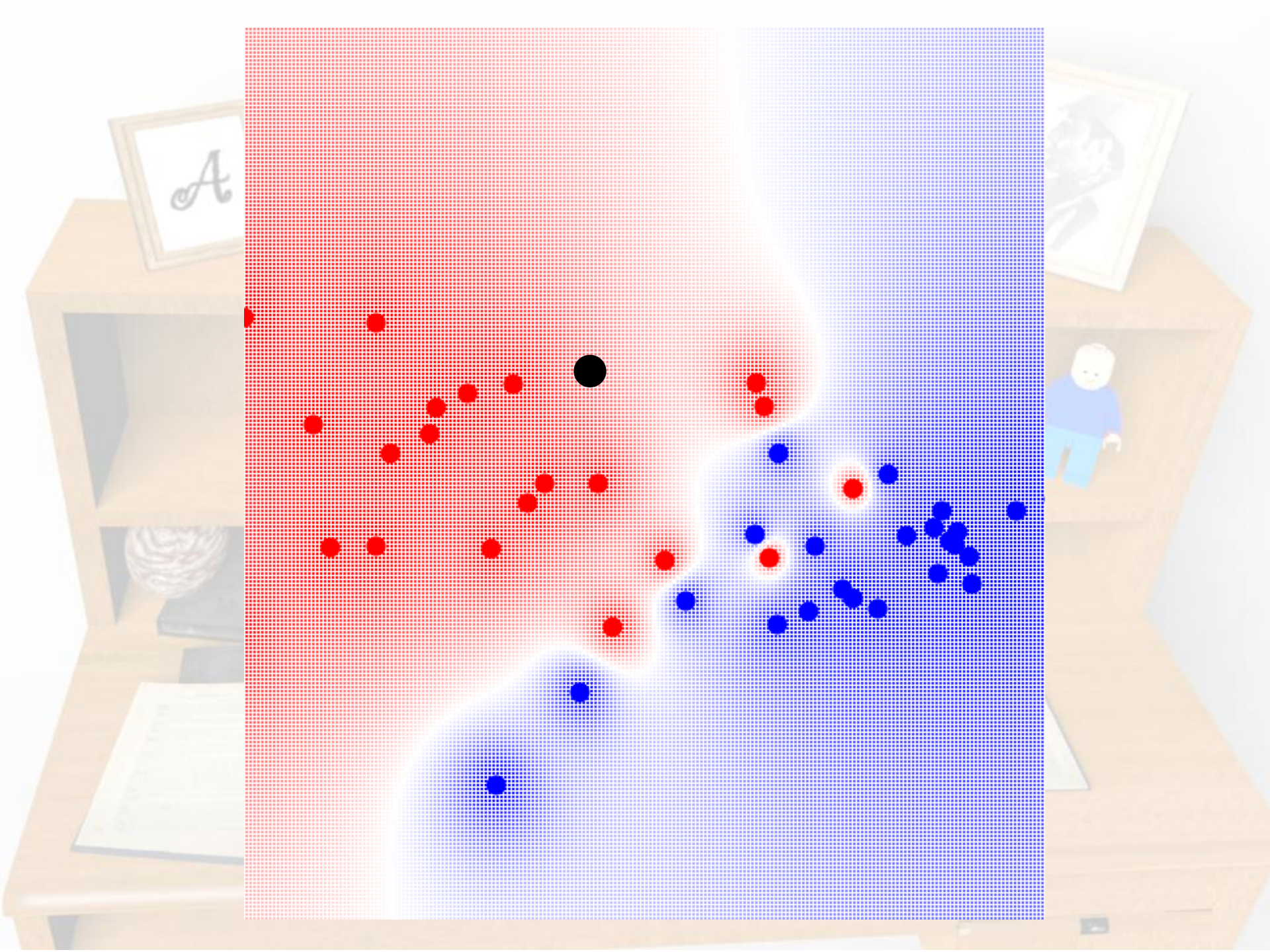
```
def classify(img):  
    distances =  
        [distance(img, p) for p in training_set]  
    i = distances.index(min(distances))  
    return training_labels[i]
```

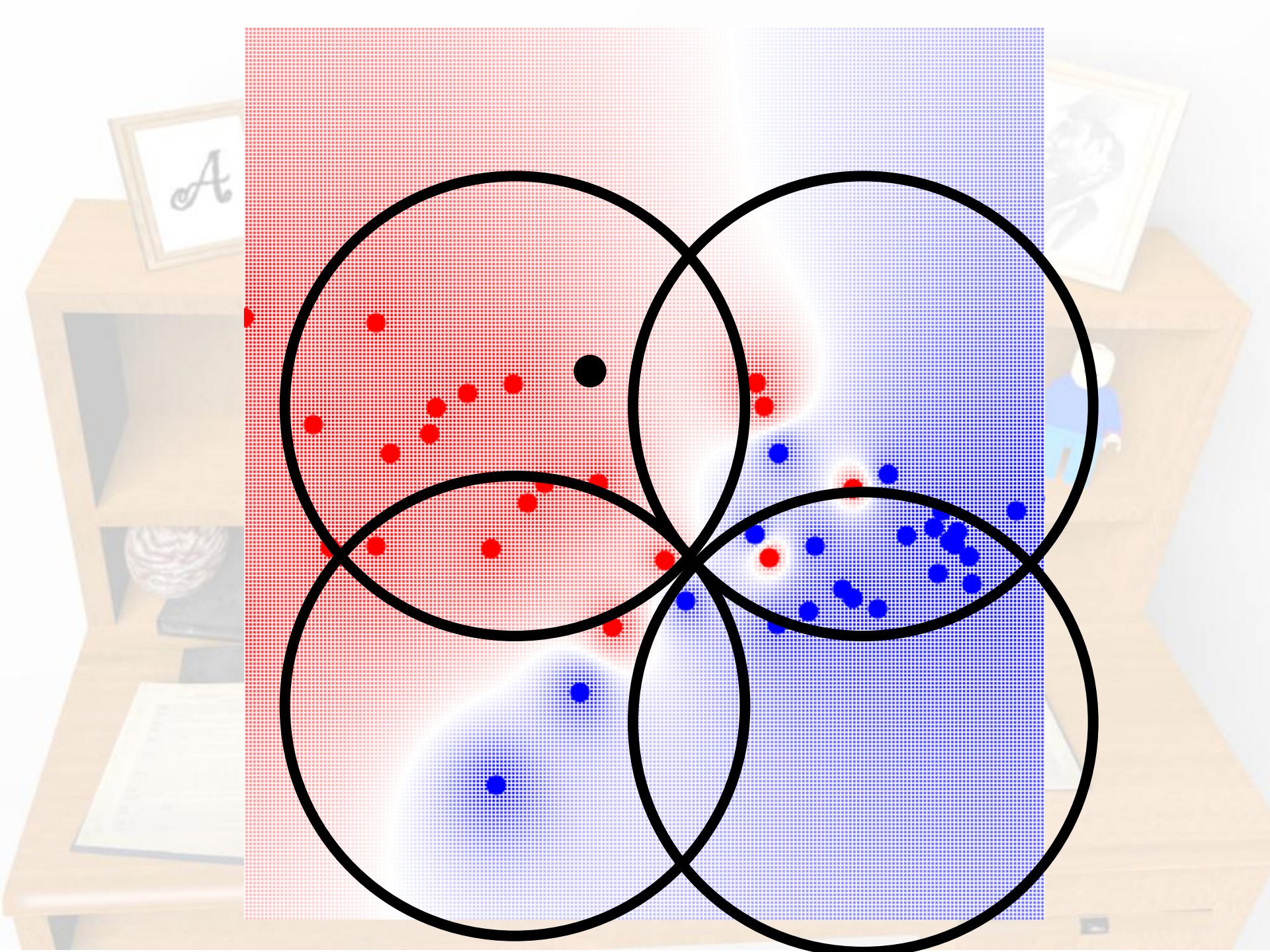
Неэффективно

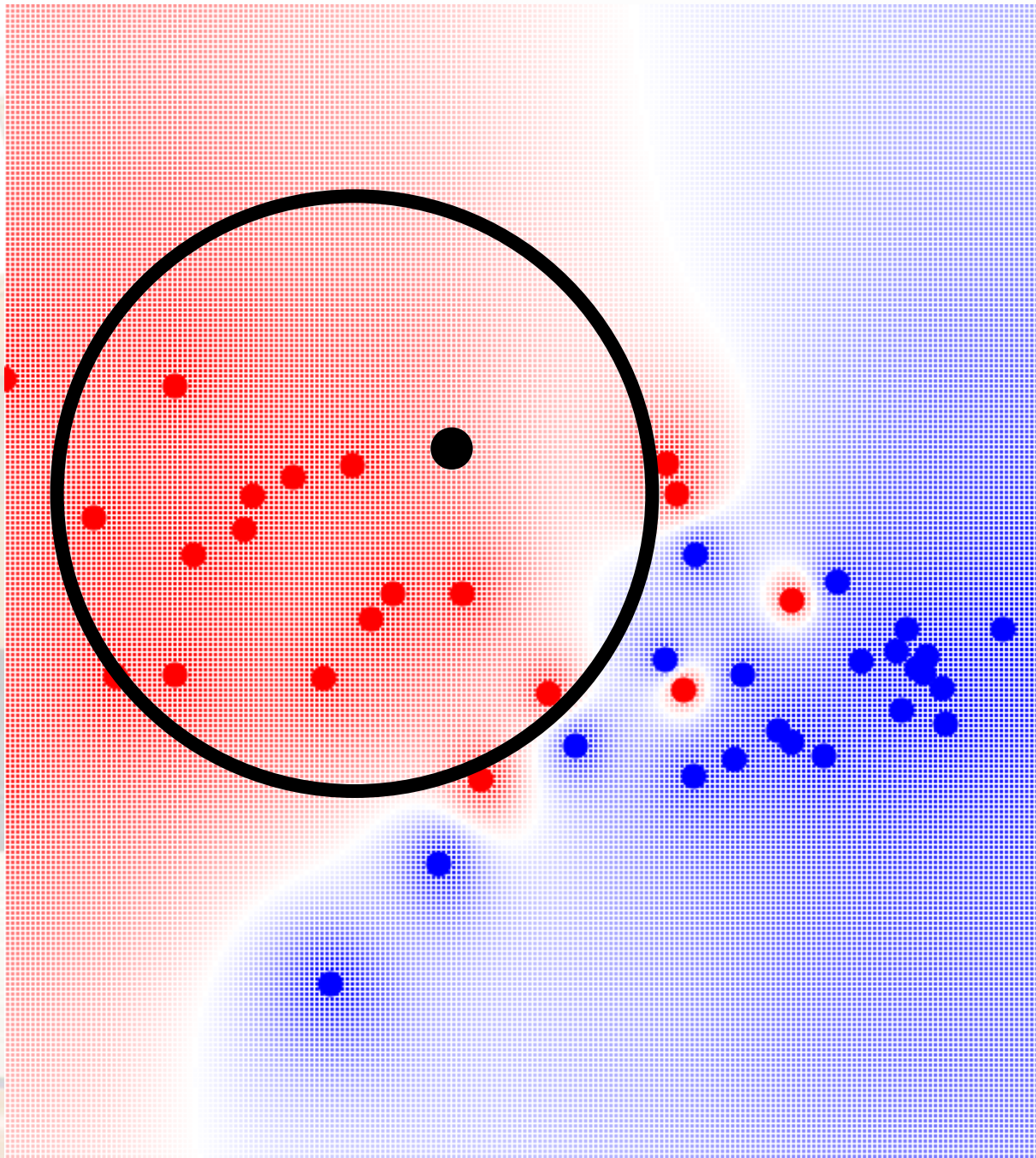
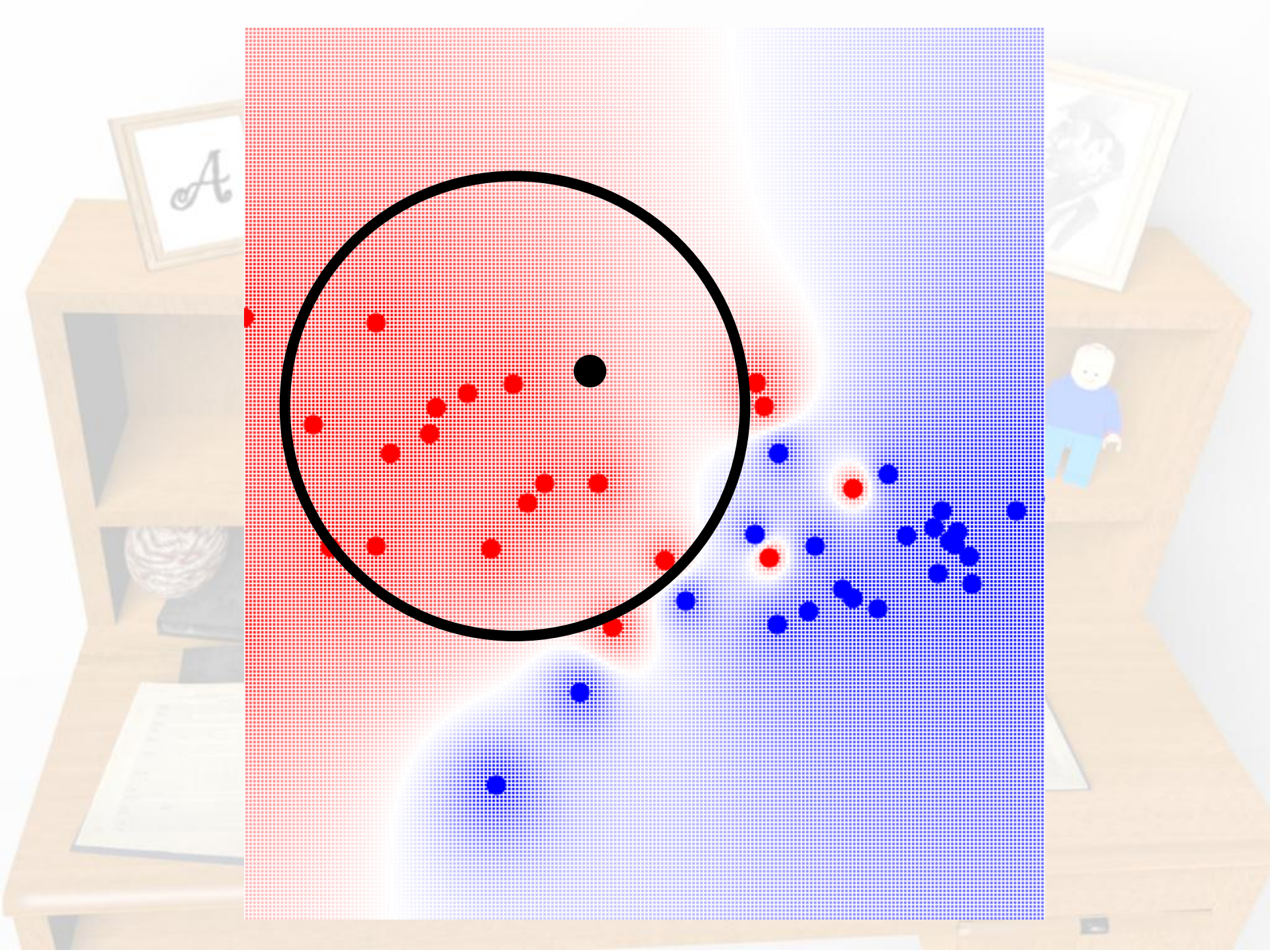
Поиск ближайшего соседа

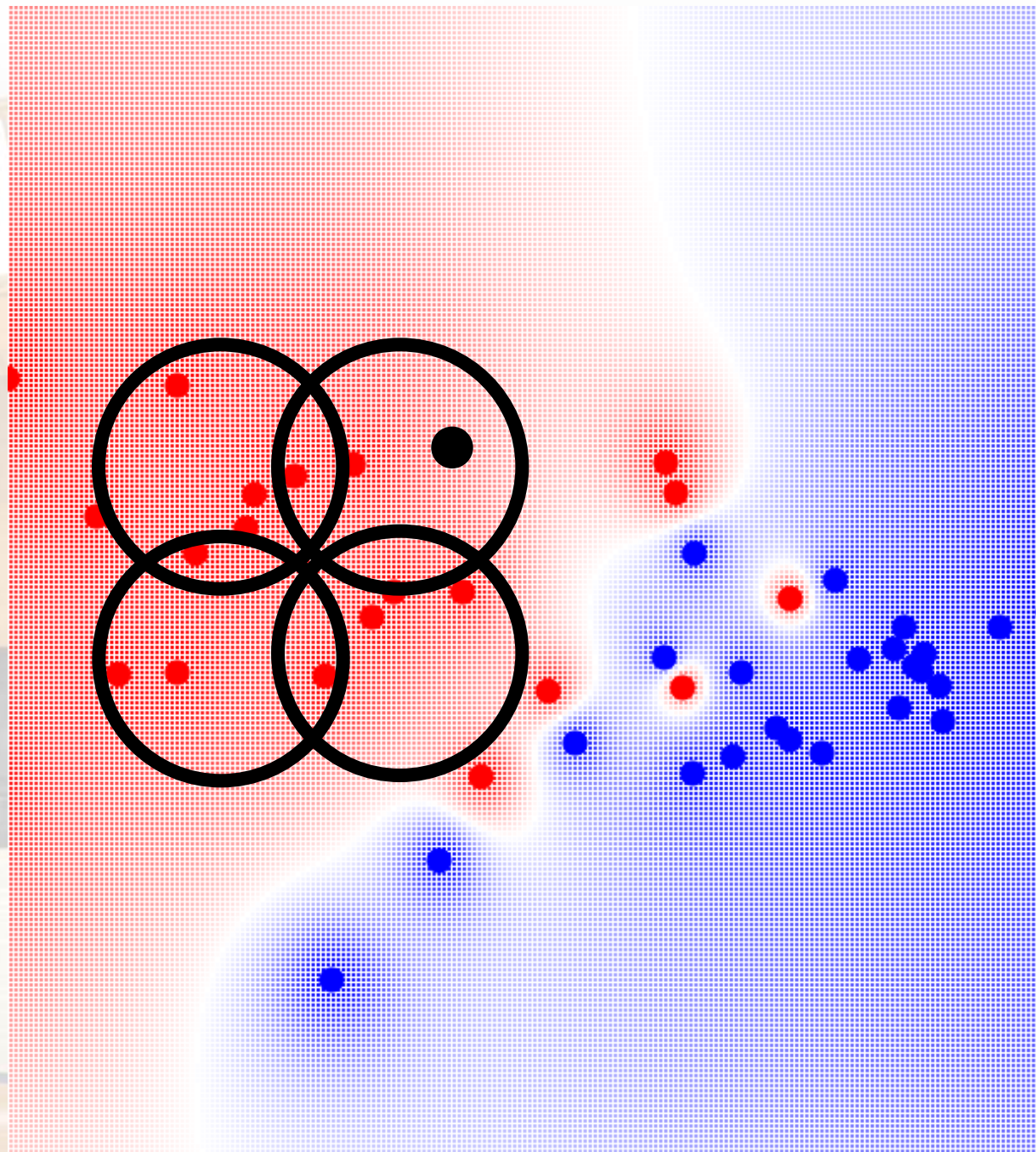
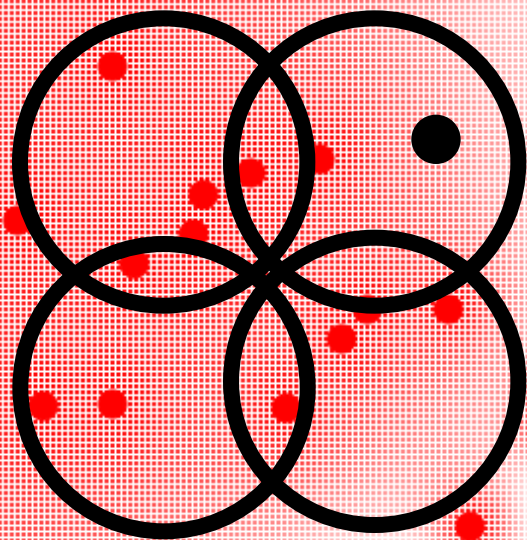
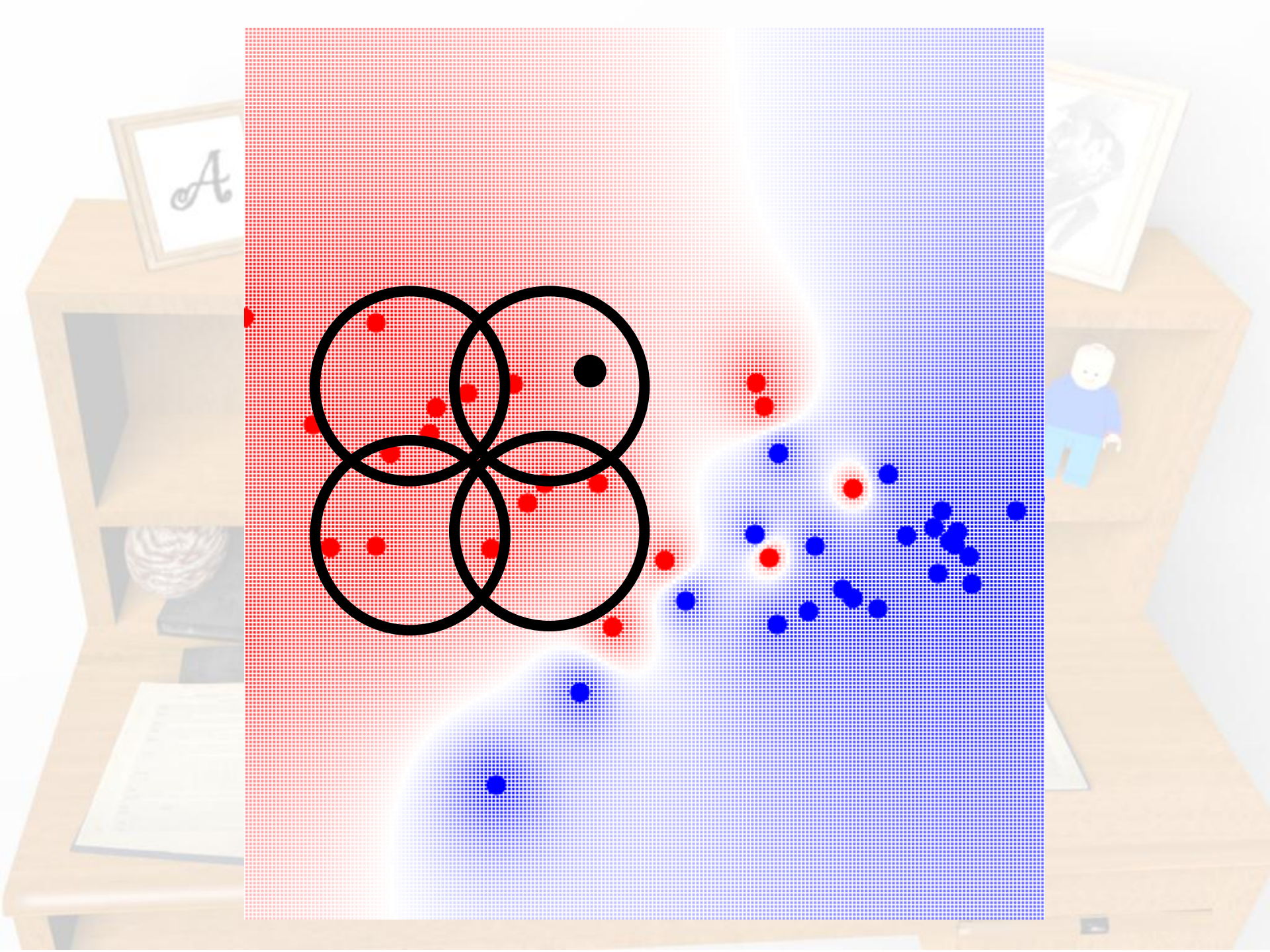
```
def classify(img):  
    nearest_neighbour =  
        training_set.find_nearest_neighbour(img)  
  
    return nearest_neighbour.label
```

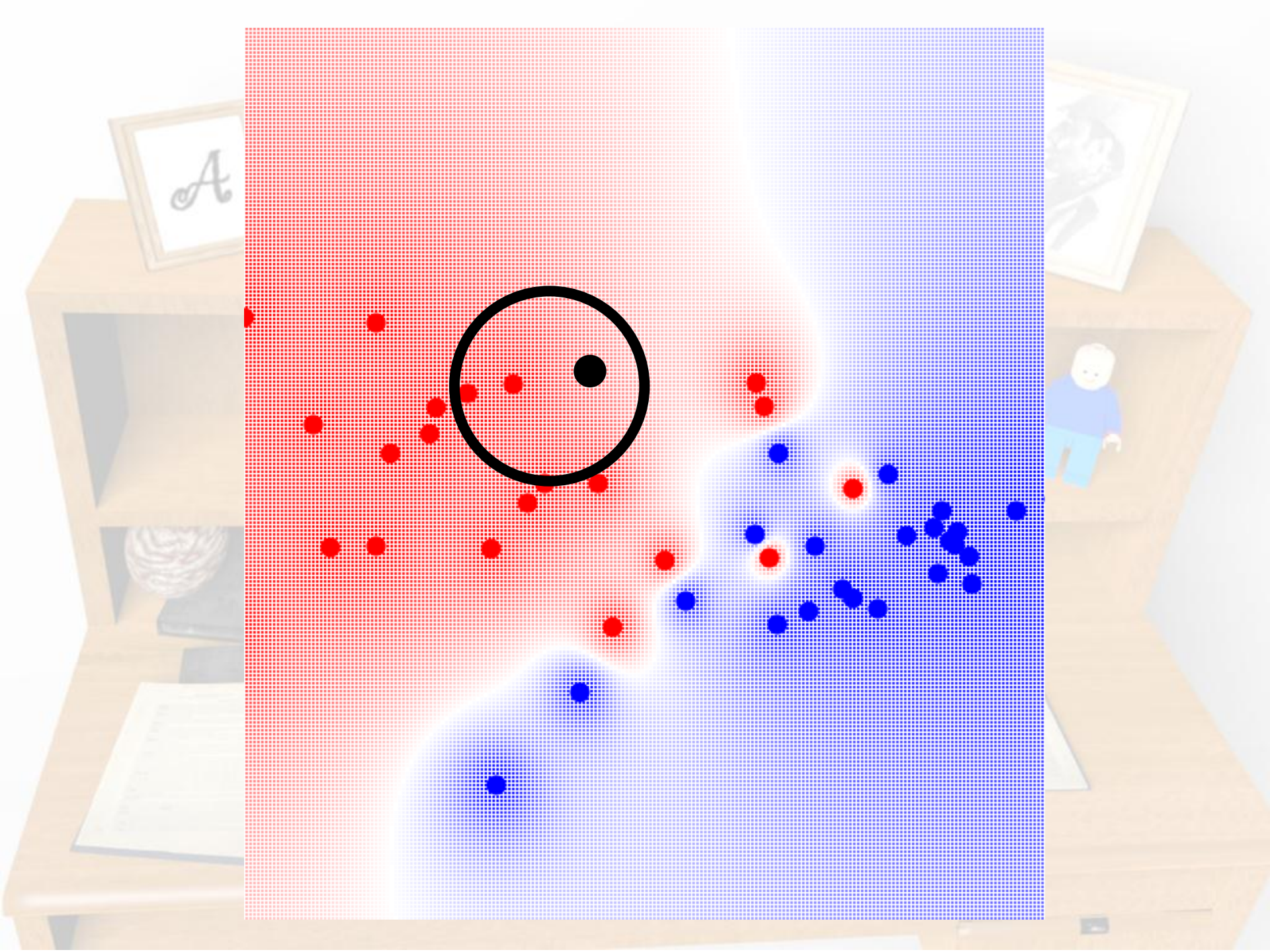
Индексирование!











find_nearest_neighbour

```
if pixel[10,13] > 4:
```

```
    if pixel[3,24] < 0:
```

```
        nearest_neighbour = A
```

```
    else:
```

```
        nearest_neighbour = B
```

```
else:
```

```
    nearest_neighbour = C
```

Classification Tree

```
if pixel[10,13] > 4:
```

```
    if pixel[3,24] < 0:
```

```
        class = '1'
```

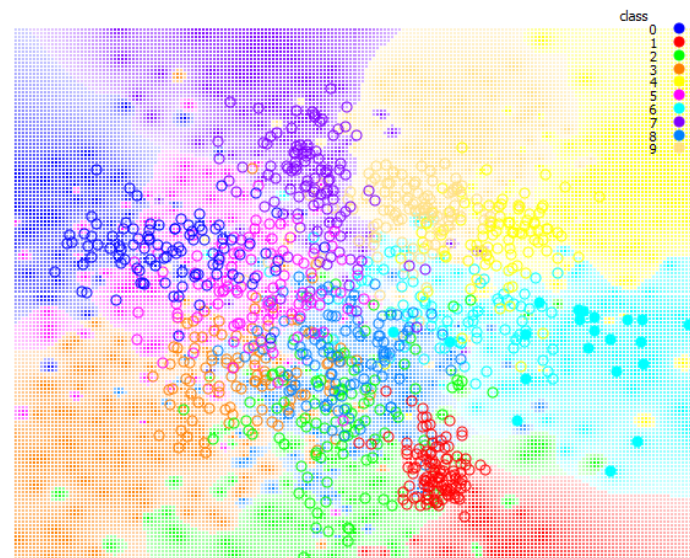
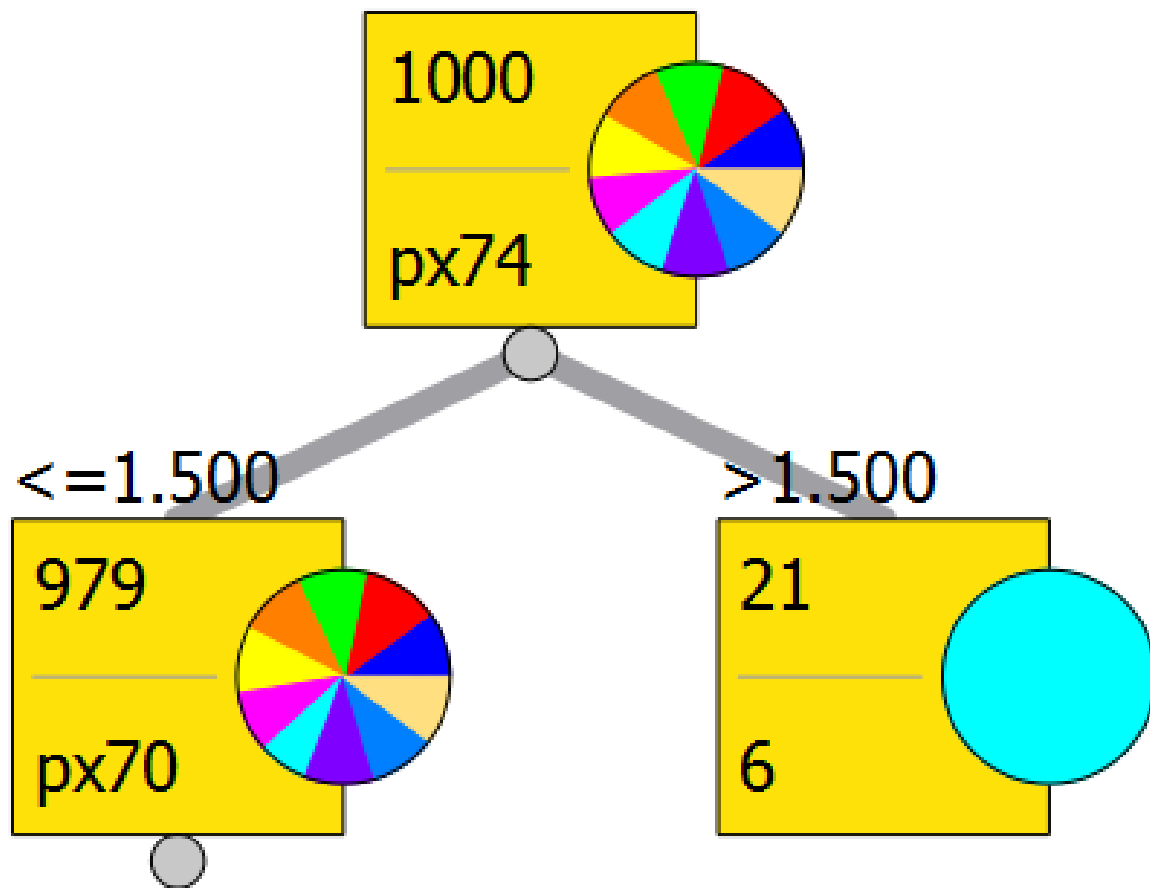
```
    else:
```

```
        class = '2'
```

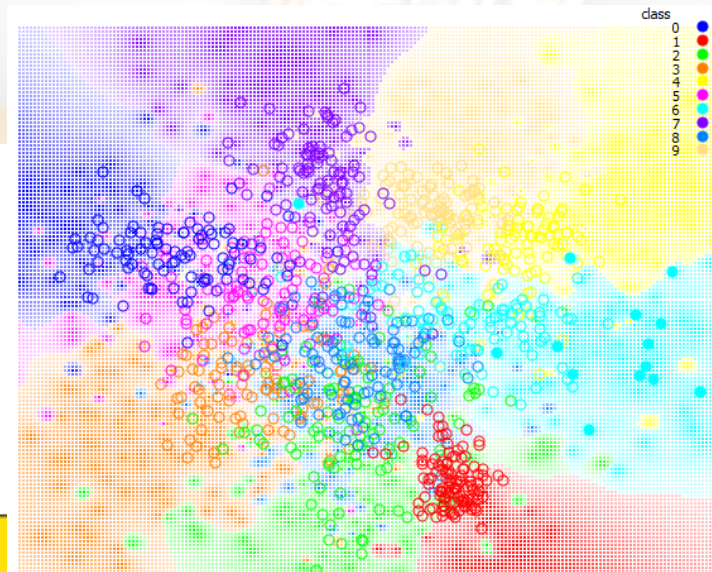
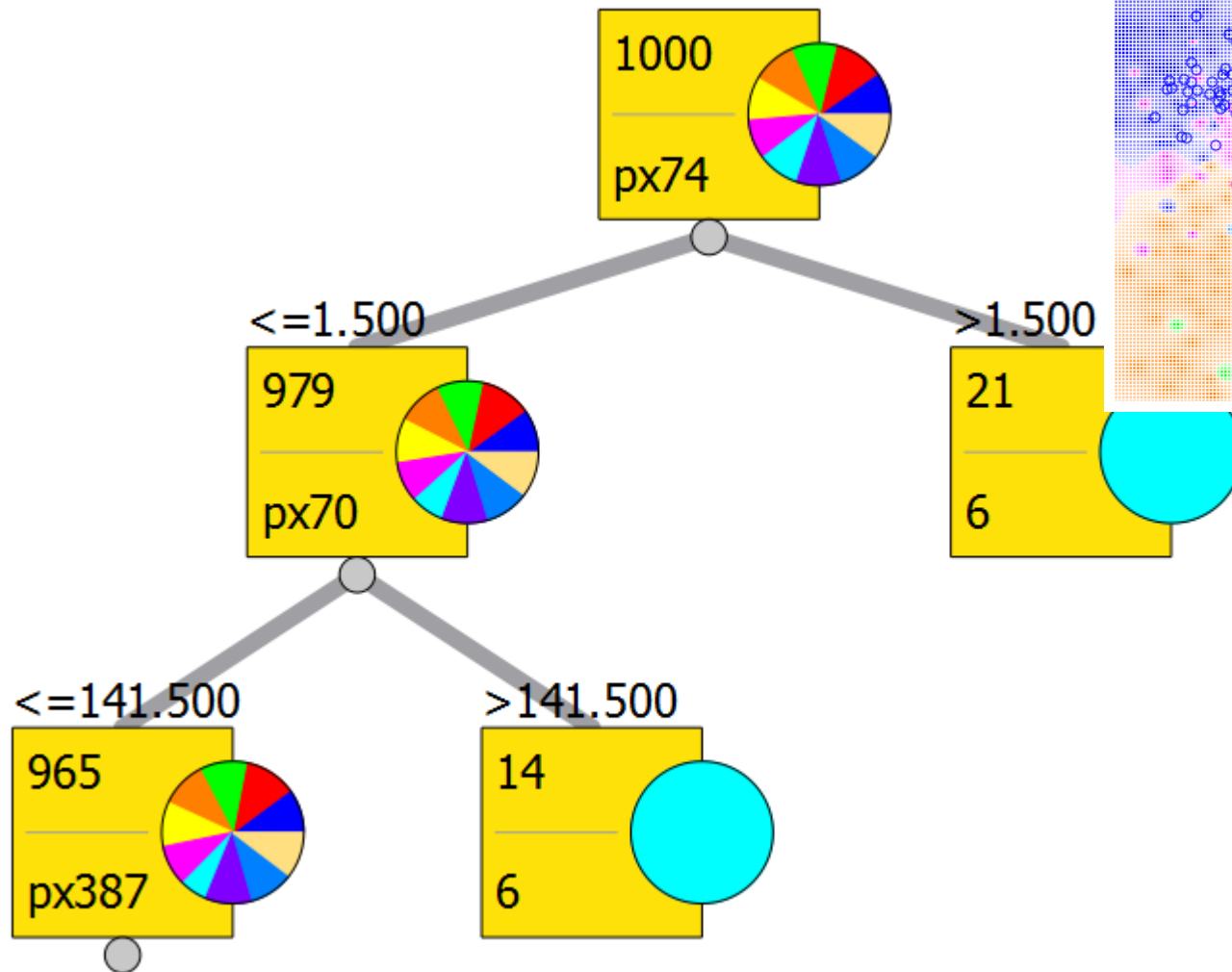
```
else:
```

```
    class = '3'
```

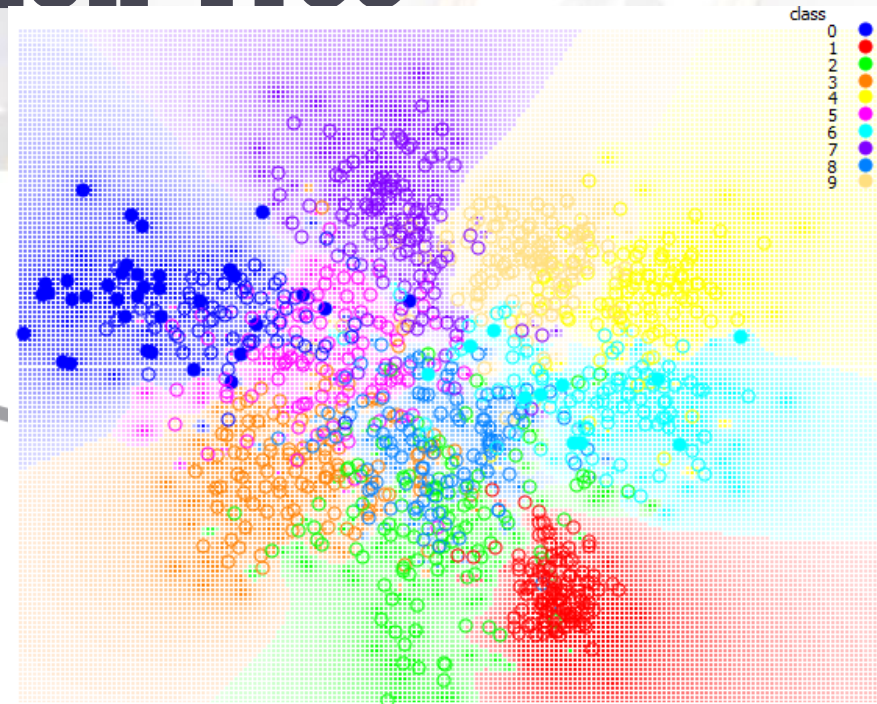
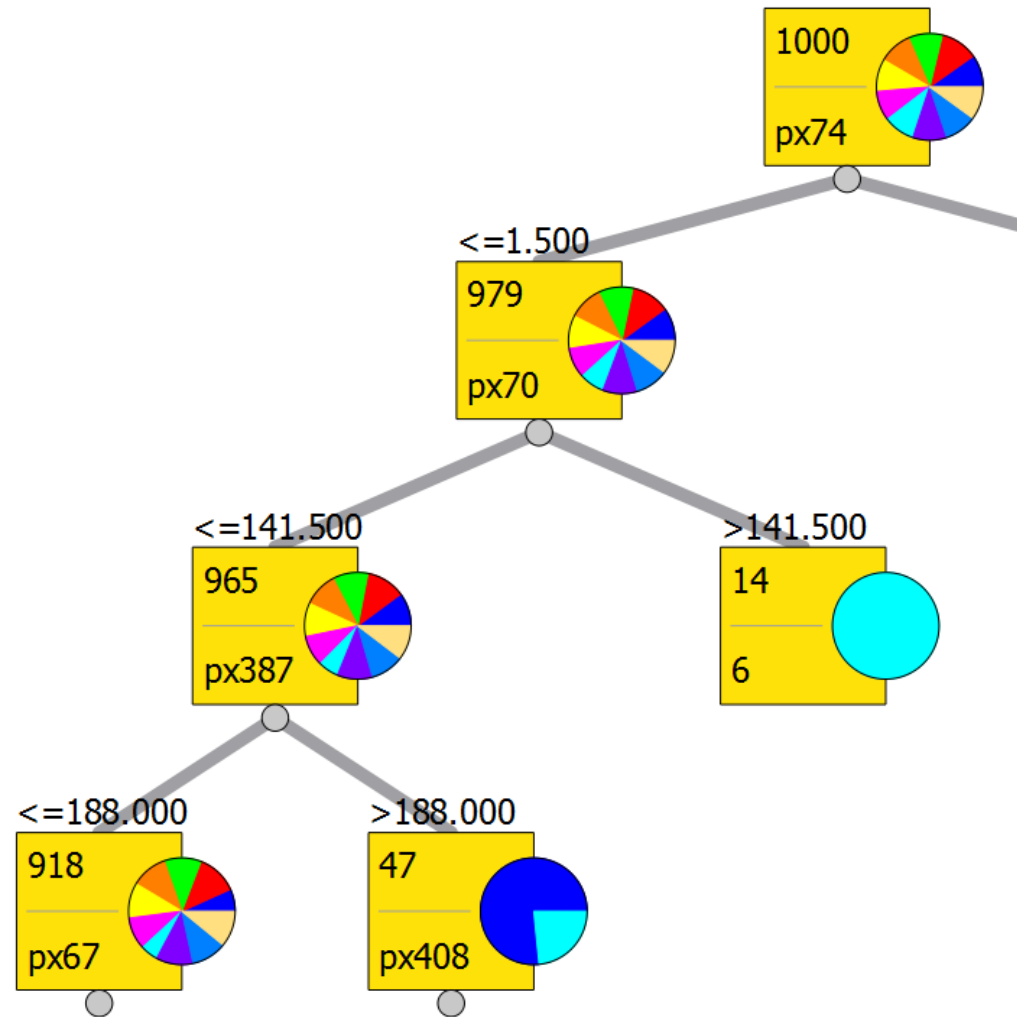
Classification Tree



Classification Tree

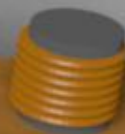


Classification Tree



Orange

<http://orange.biolab.si/>





Деревья
ID3
C4.5
RegTree

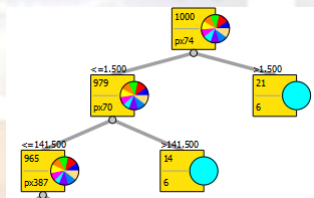
Общий вид модели

$$f(x) = \sum_i y_i w_i K(x_i, x)$$



Подбор оптимальных
параметров модели

Общий вид модели



Подбор оптимального
дерева



Моделирование



Оптимизация

Линейная модель

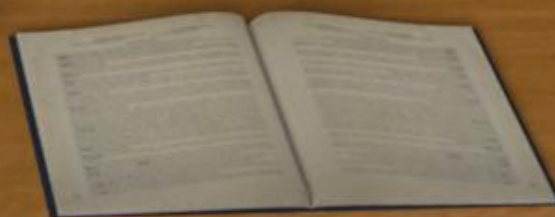
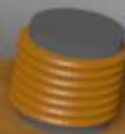
$f(\text{image}) =$

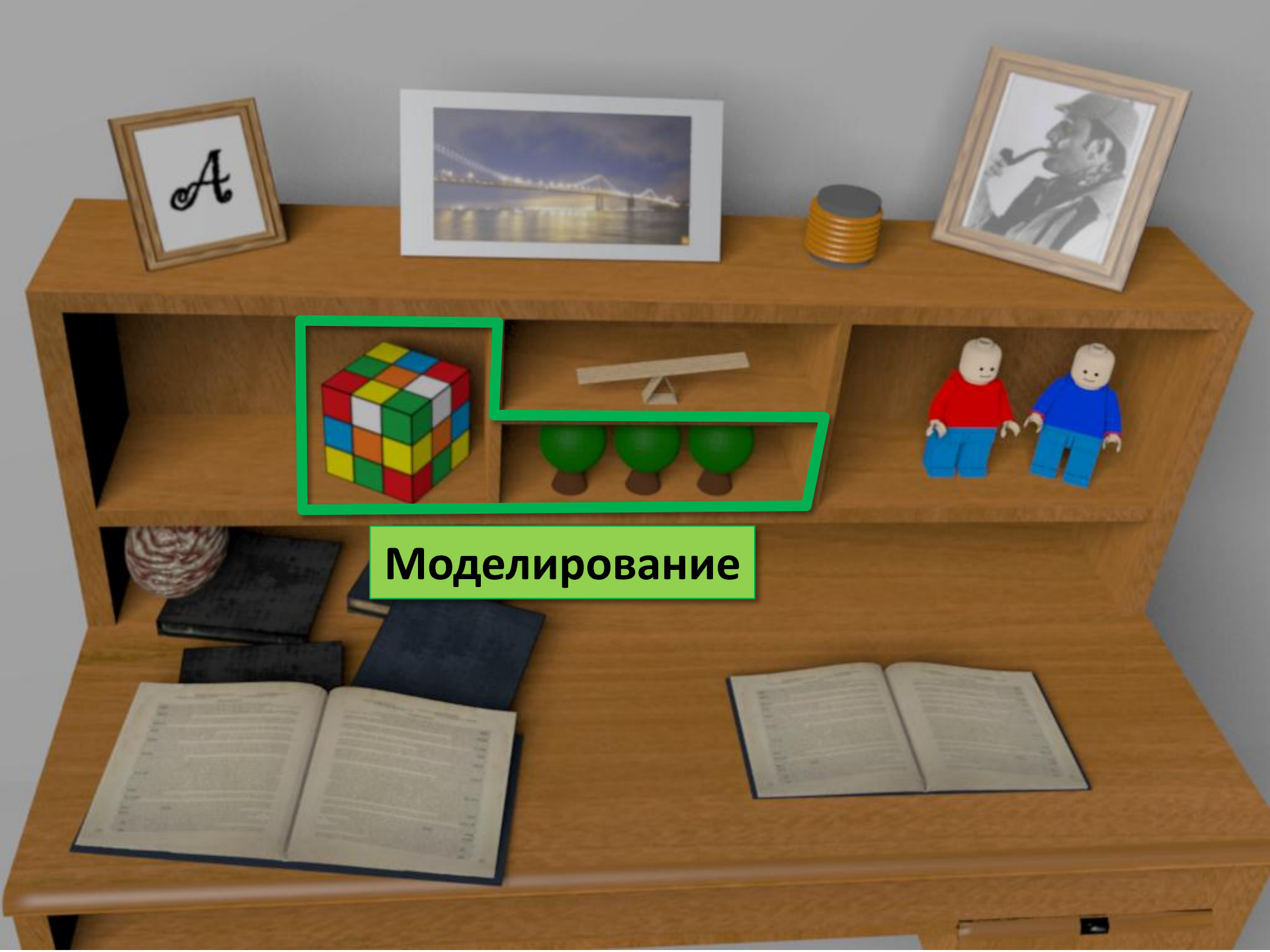
$\text{pixel1} * w1 + \text{pixel2} * w2 + \dots + \text{pixel784} * w784$

Linear Classification

```
from sklearn.linear_model import  
    LinearRegression,  
    LogisticRegression,  
    RidgeClassifier,  
    LARS,  
    ElasticNet,  
    SGDClassifier,  
    ...
```

=> 809/1000





Моделирование

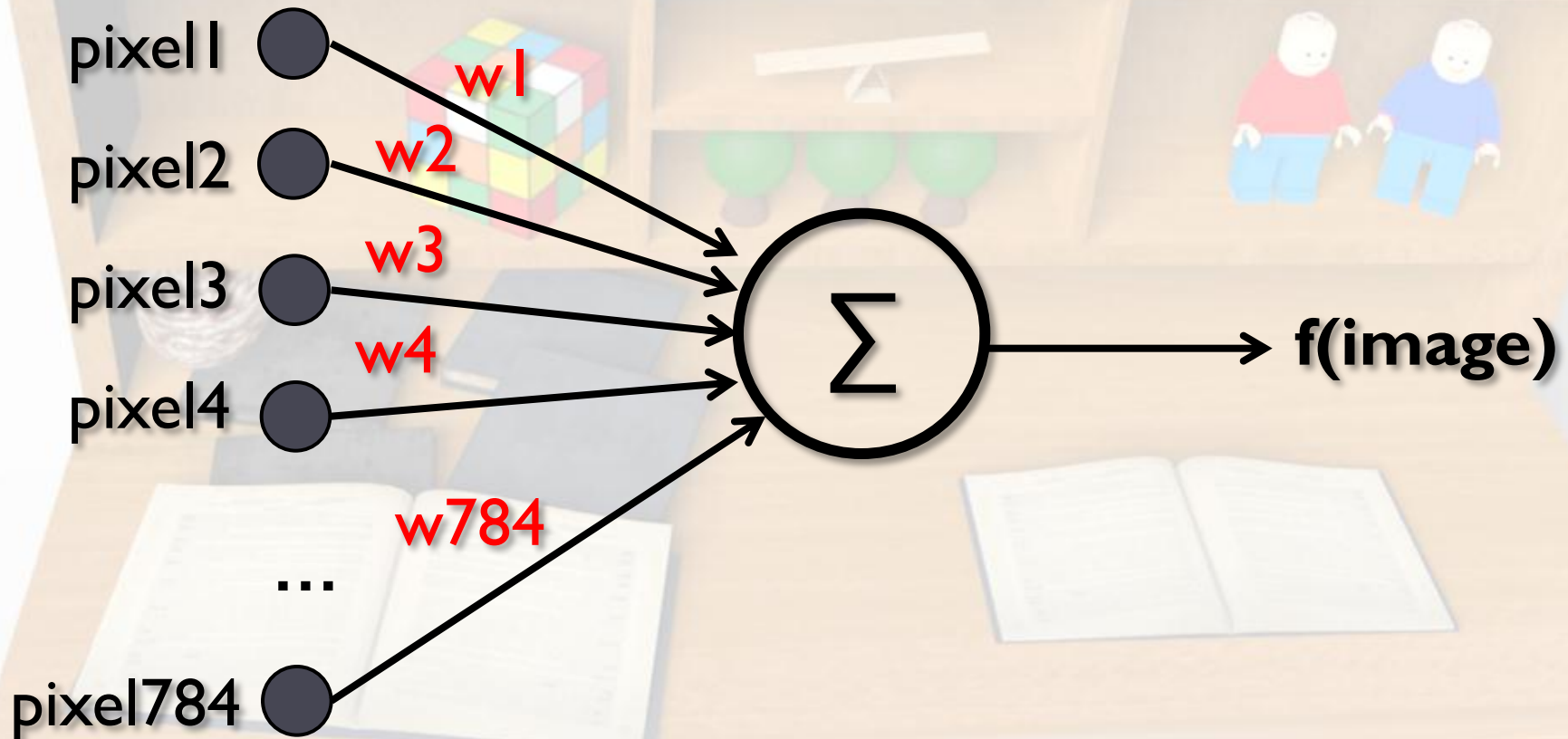
Линейная модель

$f(\text{image}) =$

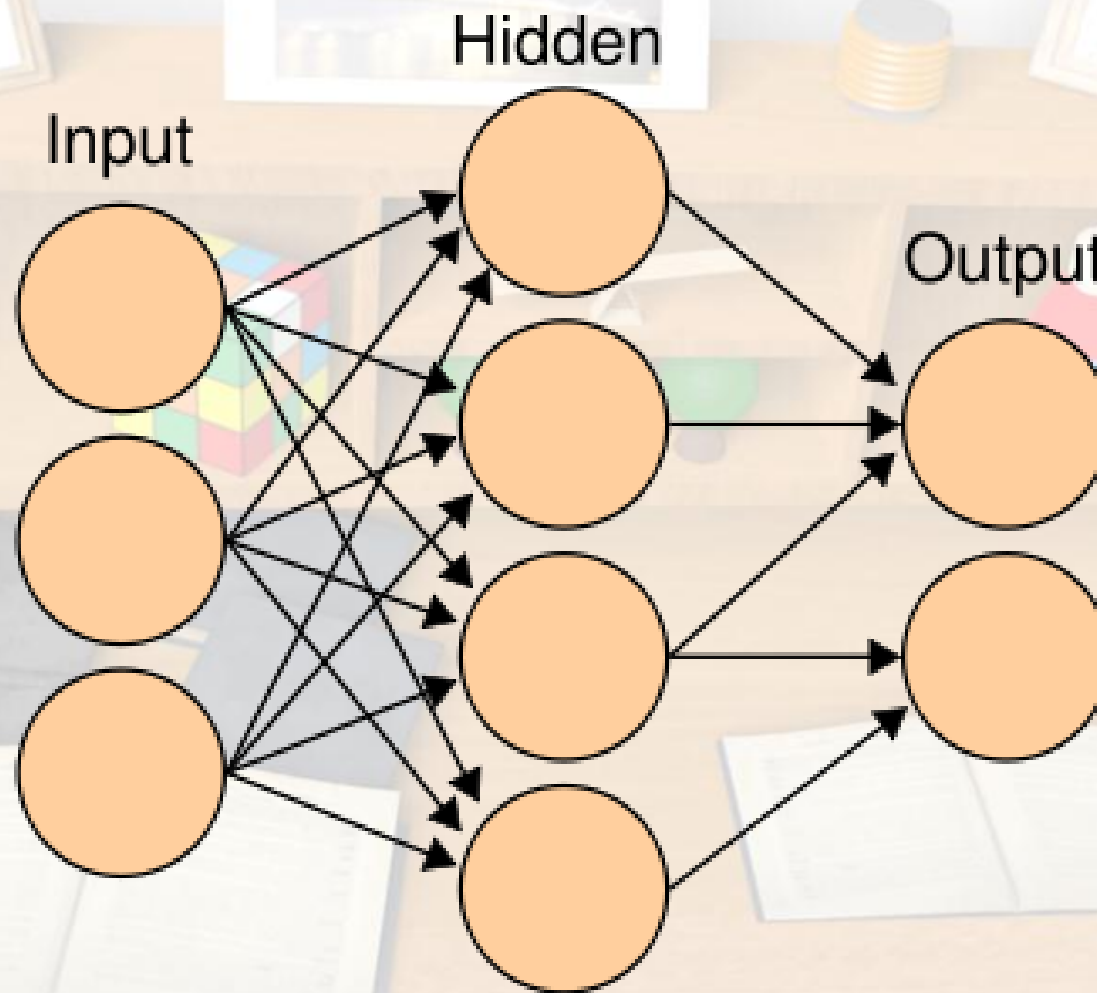
$\text{pixel1} * w1 + \text{pixel2} * w2 + \dots + \text{pixel784} * w784$

$f(\text{image}) =$

$$\text{pixel1} * w1 + \text{pixel2} * w2 + \dots + \text{pixel784} * w784$$



Нейронная сеть

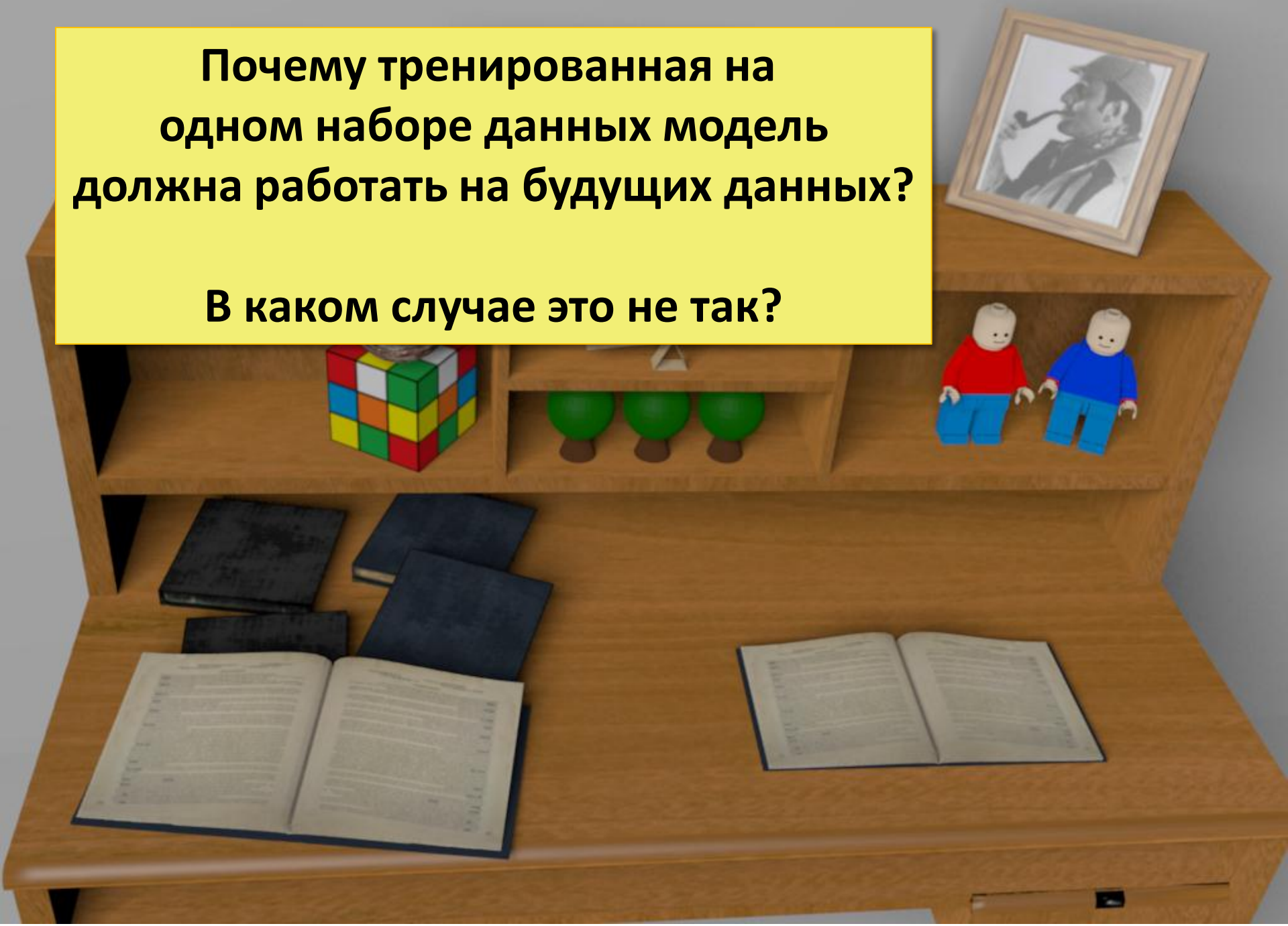


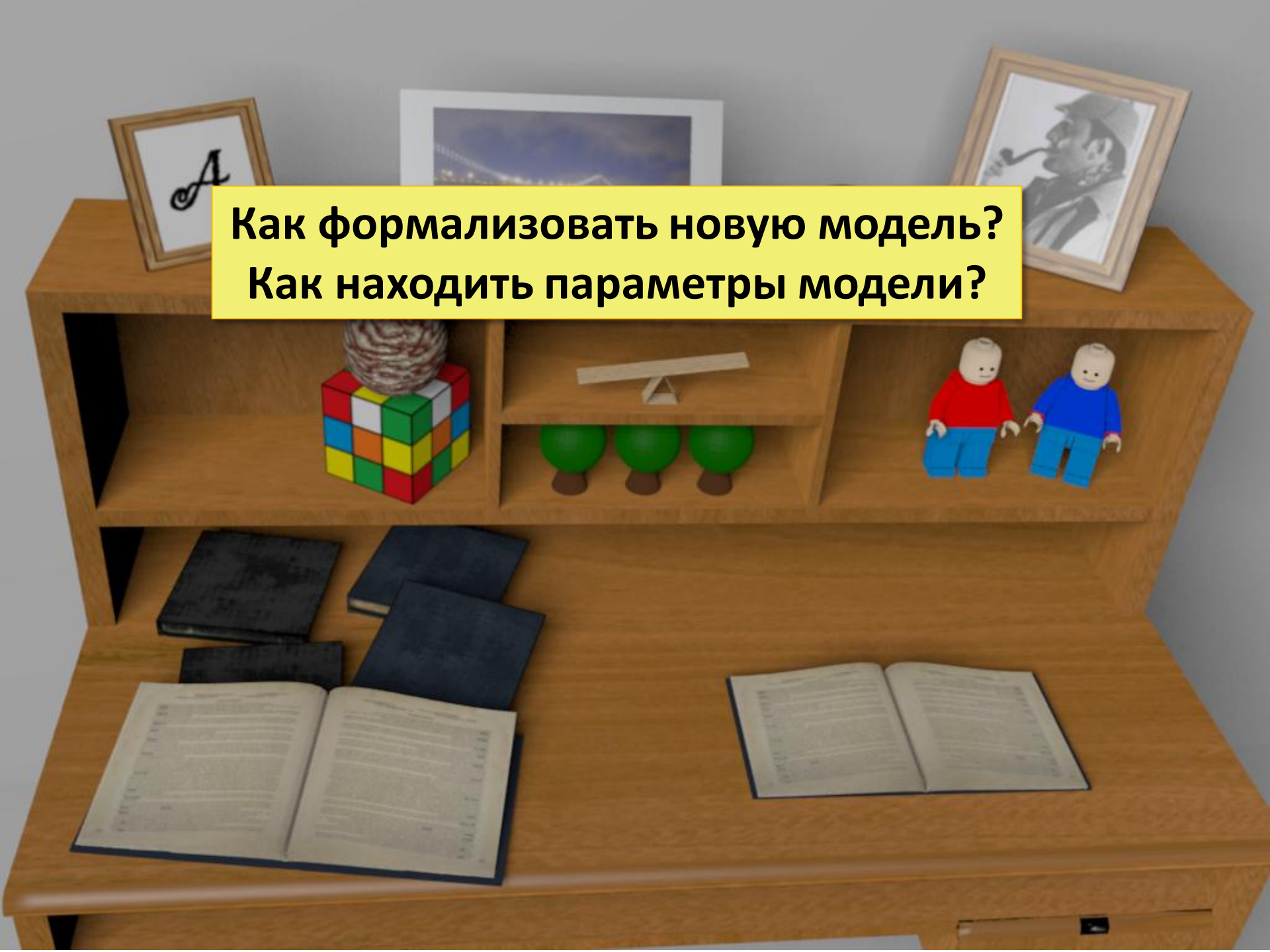


Моделирование

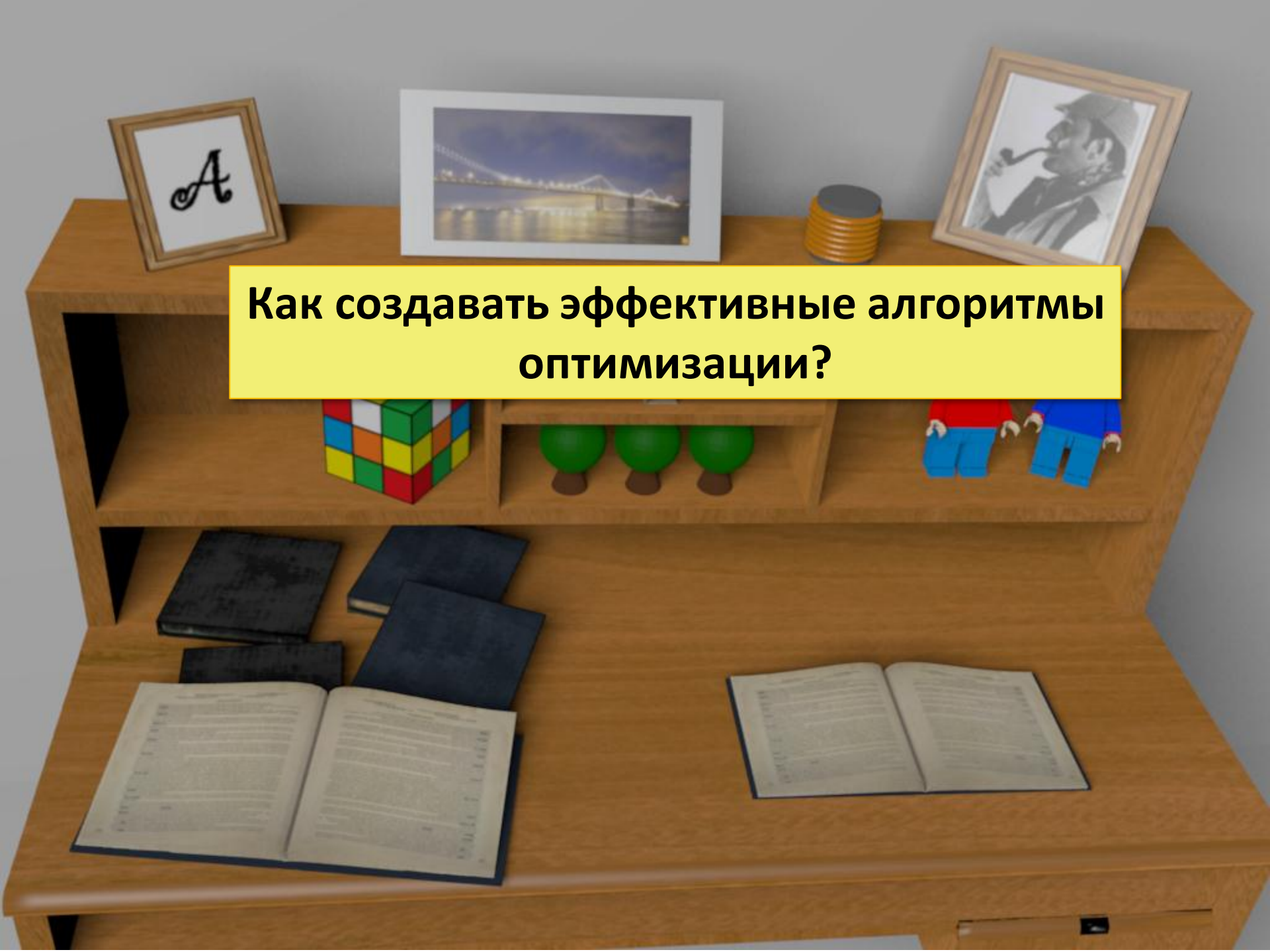
**Почему тренированная на
одном наборе данных модель
должна работать на будущих данных?**

В каком случае это не так?

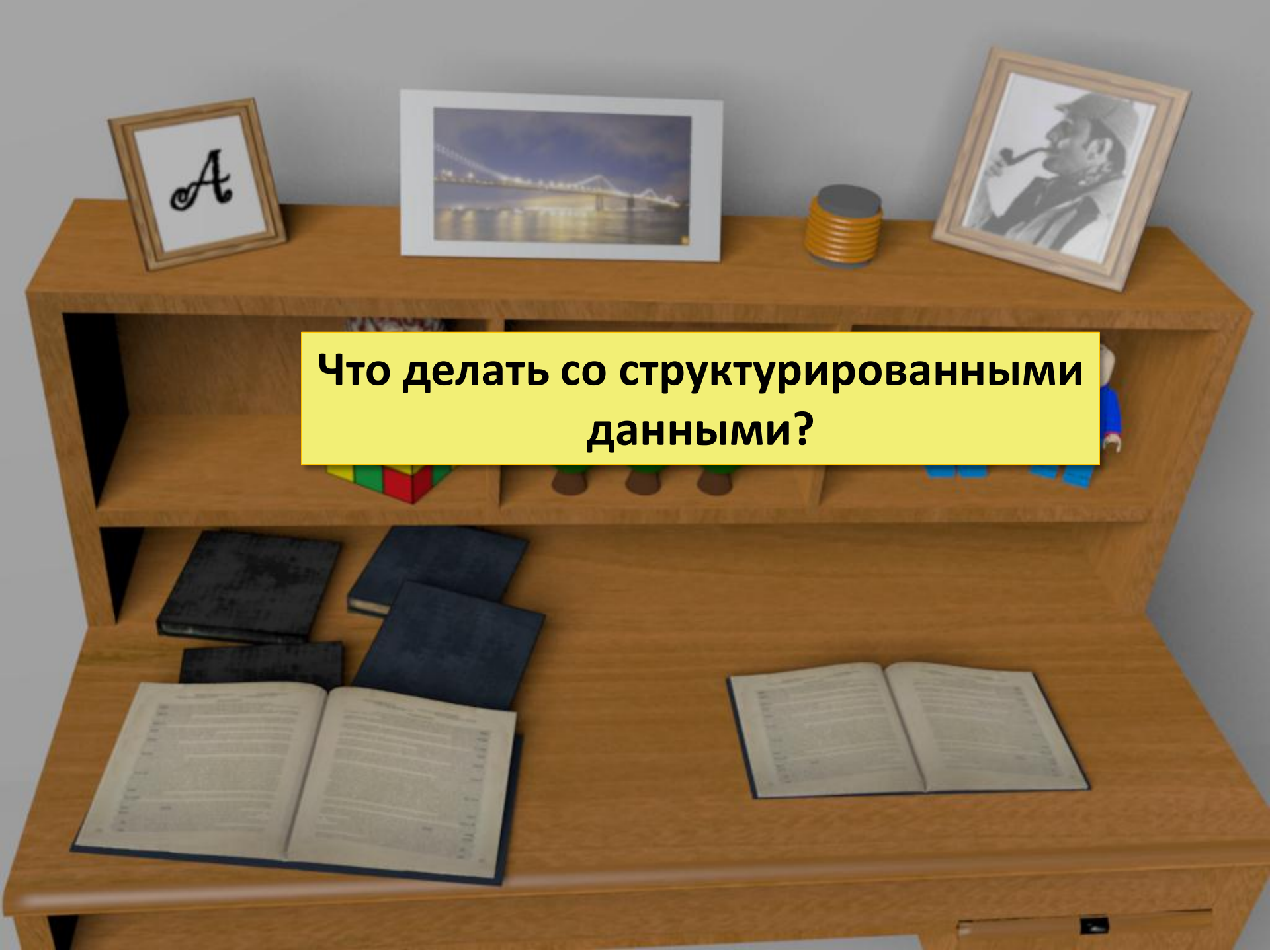




**Как формализовать новую модель?
Как находить параметры модели?**



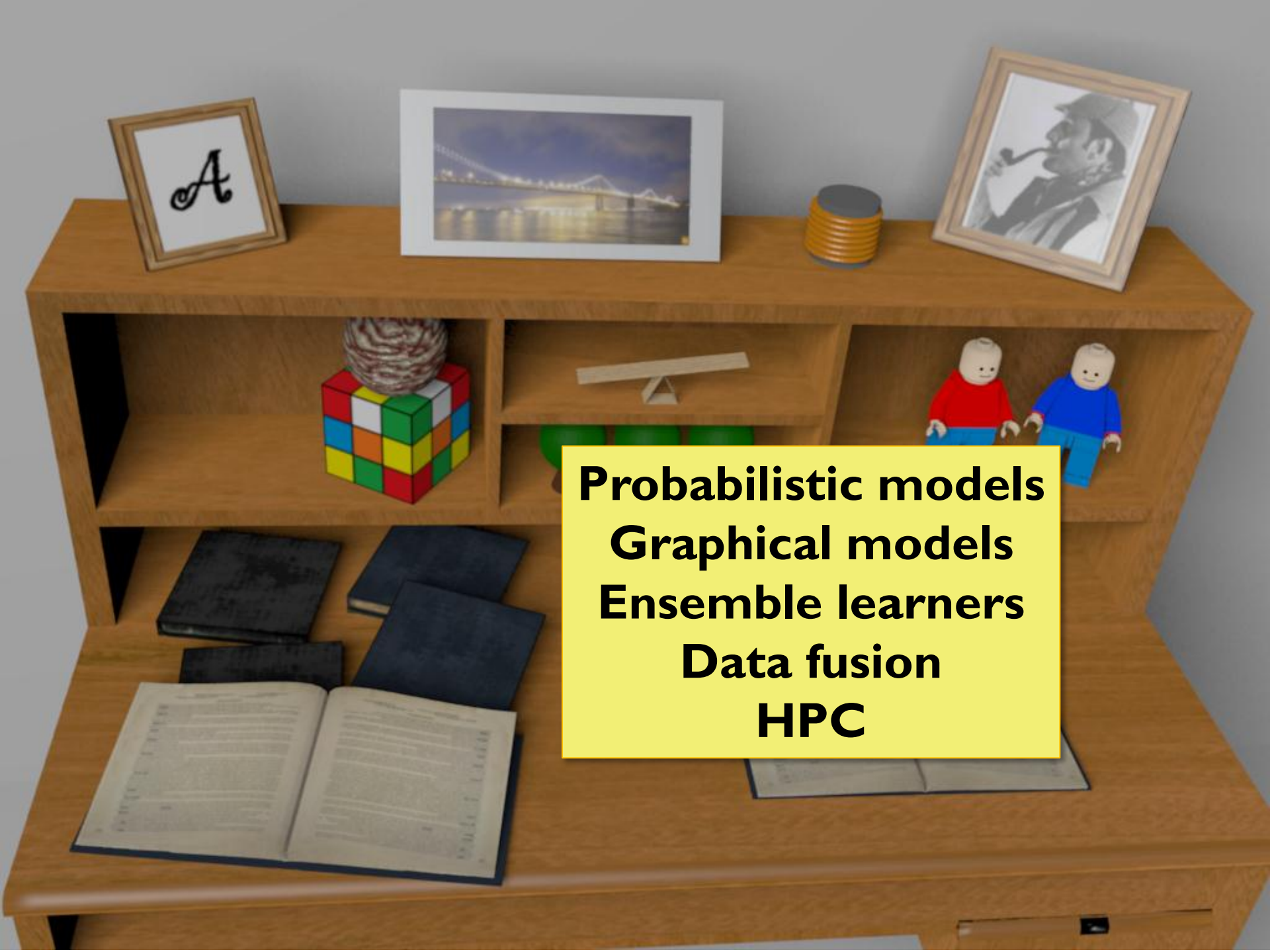
**Как создавать эффективные алгоритмы
оптимизации?**

A wooden desk with a shelf above it. On the shelf are three framed pictures: a letter 'A', a bridge at night, and a man smoking a pipe. There is also a stack of yellow and orange coasters. On the desk surface, there are several books, some open and some closed. A yellow text box is centered on the desk.

Что делать со структурированными данными?



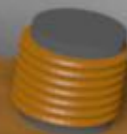
Unsupervised learning
Semi-supervised learning
On-line learning
Active learning
Multi-instance learning
Reinforcement learning

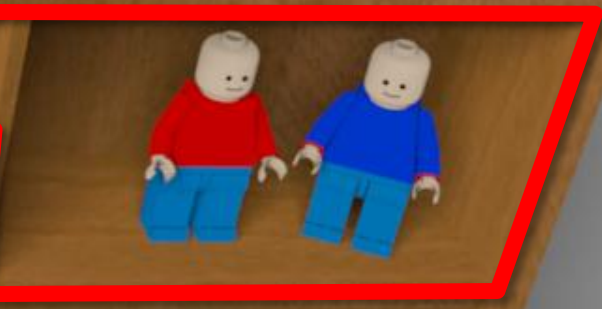


Probabilistic models
Graphical models
Ensemble learners
Data fusion
HPC



**Инструменты:
R, Weka, RapidMiner,
Orange, scikits-learn,
MLPy, MDP, PyBrain, ...**







Вопросы?